

# Computer Animation

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CS 4810: Graphics

Acknowledgment: slides by Jason Lawrence, Misha Kazhdan, Allison Klein, Tom Funkhouser, Adam Finkelstein and David Dobkin

# Overview

- Some early animation history
  - [http://en.wikipedia.org/wiki/History\\_of\\_animation#Animation\\_before\\_film](http://en.wikipedia.org/wiki/History_of_animation#Animation_before_film)
- Computer animation

# Thaumatrope

- Why does animation work?
- Persistence of vision
- 1824 John Ayerton invents the *thaumatrope*
- Or, 1828 Paul Roget invents the *thaumatrope*



Thaumatrope

# Thaumatrope

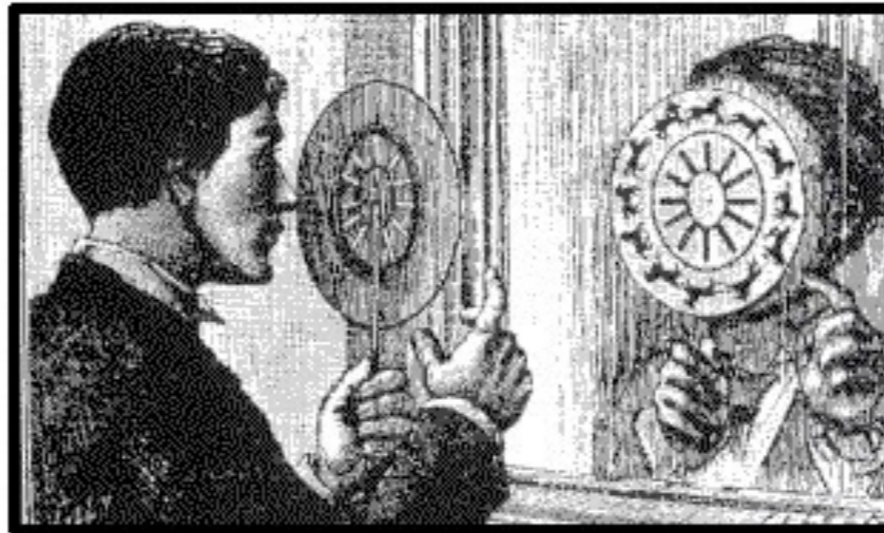
- Why does animation work?
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- Or, 1828 Paul Roget invents the *thaumatrope*



Thaumatrope

# Phenakistoscope

- Invented independently by 2 people in 1832
- Disc mounted on spindle
- Viewed through slots with images facing mirror
- Turning disc animates images



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# Zoetrope (1834)

- Images arranged on paper band inside a drum
- Slits cut in the upper half of the drum
- Opposite side viewed as drum rapidly spun
- Praxinoscope is a variation on this





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# Mutoscope (1895)

- Coin-operated “flip-book” animation
- Picture cards attached to a drum
- Popular at sea-side resorts, etc.

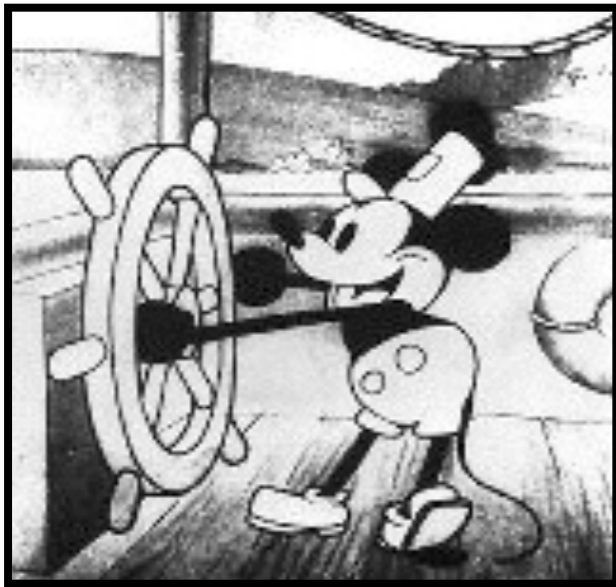


# Animation History

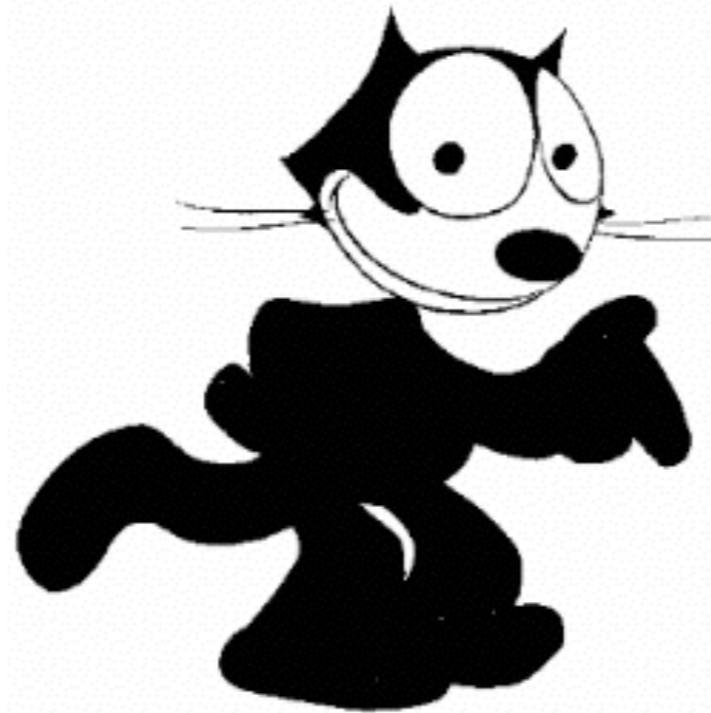
- Animation and technology have always gone together!
- Animation popular even before movies
- Movies were big step forward!
- "Humorous Phases of Funny Faces" (1906)

# Key Developments

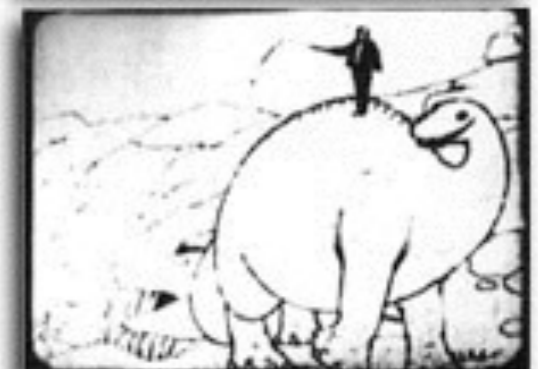
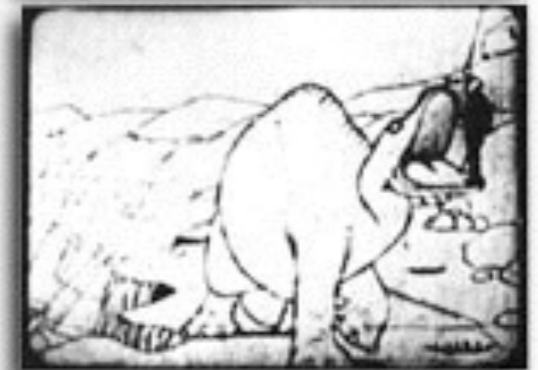
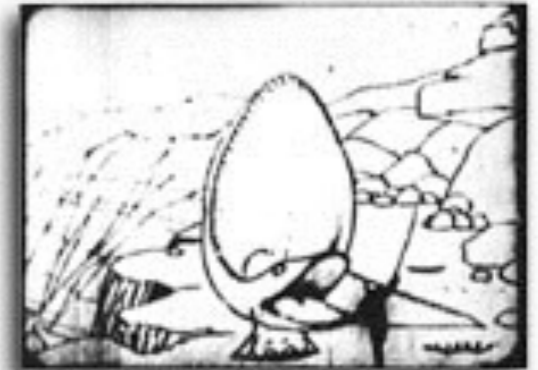
- Plot
- Creation of animation studios
- Getting rid of “rubber-hose” bodies
- Inking on cels



“Steamboat Willie”  
Walt Disney (1928)



“Felix the Cat”  
Pat Sullivan (1919)

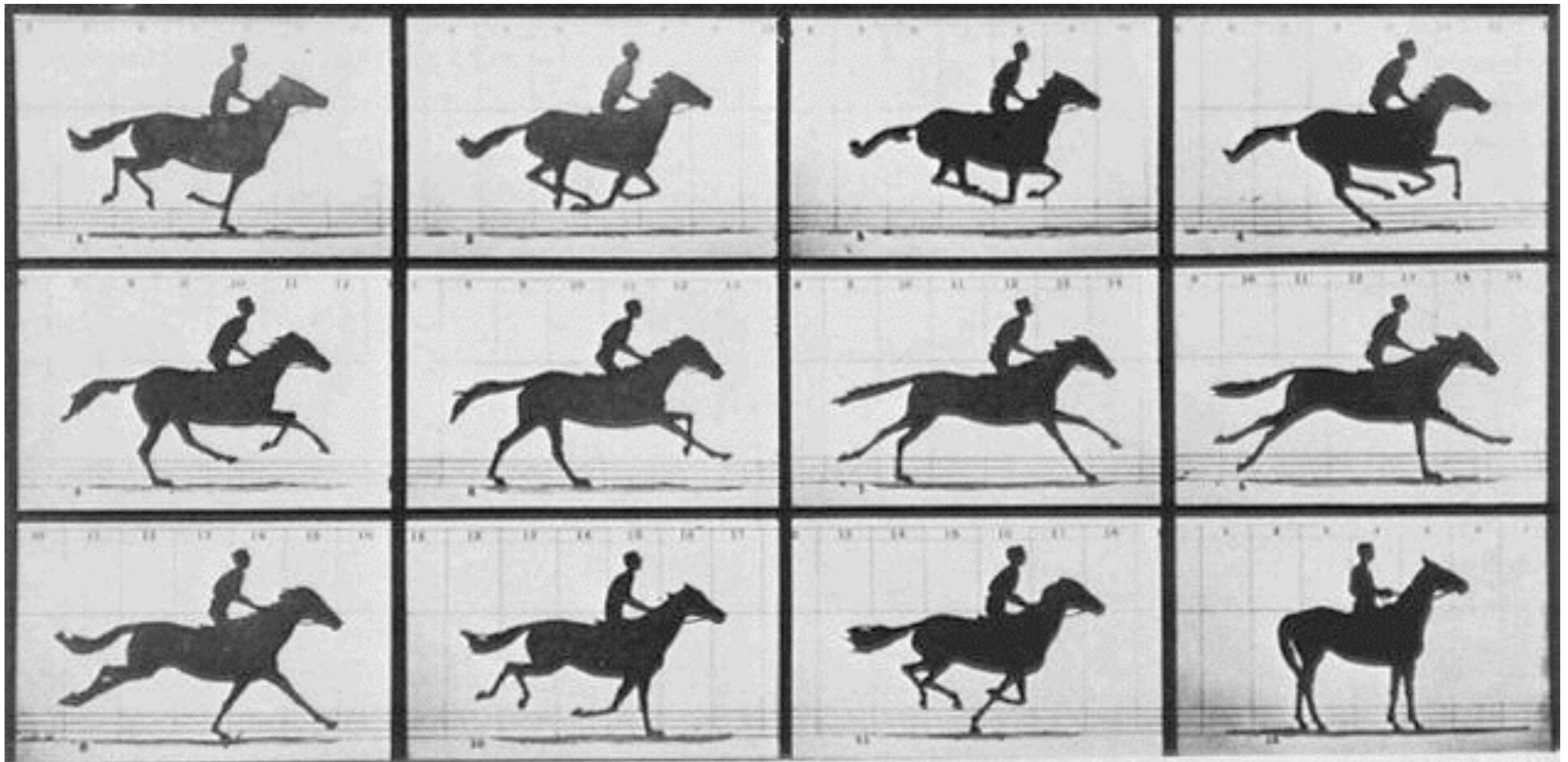


“Gertie the Dinosaur”  
Windsor McCay (1914)



# Key Developments

- Max Fleischer invents rotoscoping (1921)



Copyright, 1878, by MUYBRIDGE.

MORSE'S Gallery, 417 Montgomery St., San Francisco.

## THE HORSE IN MOTION.

Illustrated by  
MUYBRIDGE.

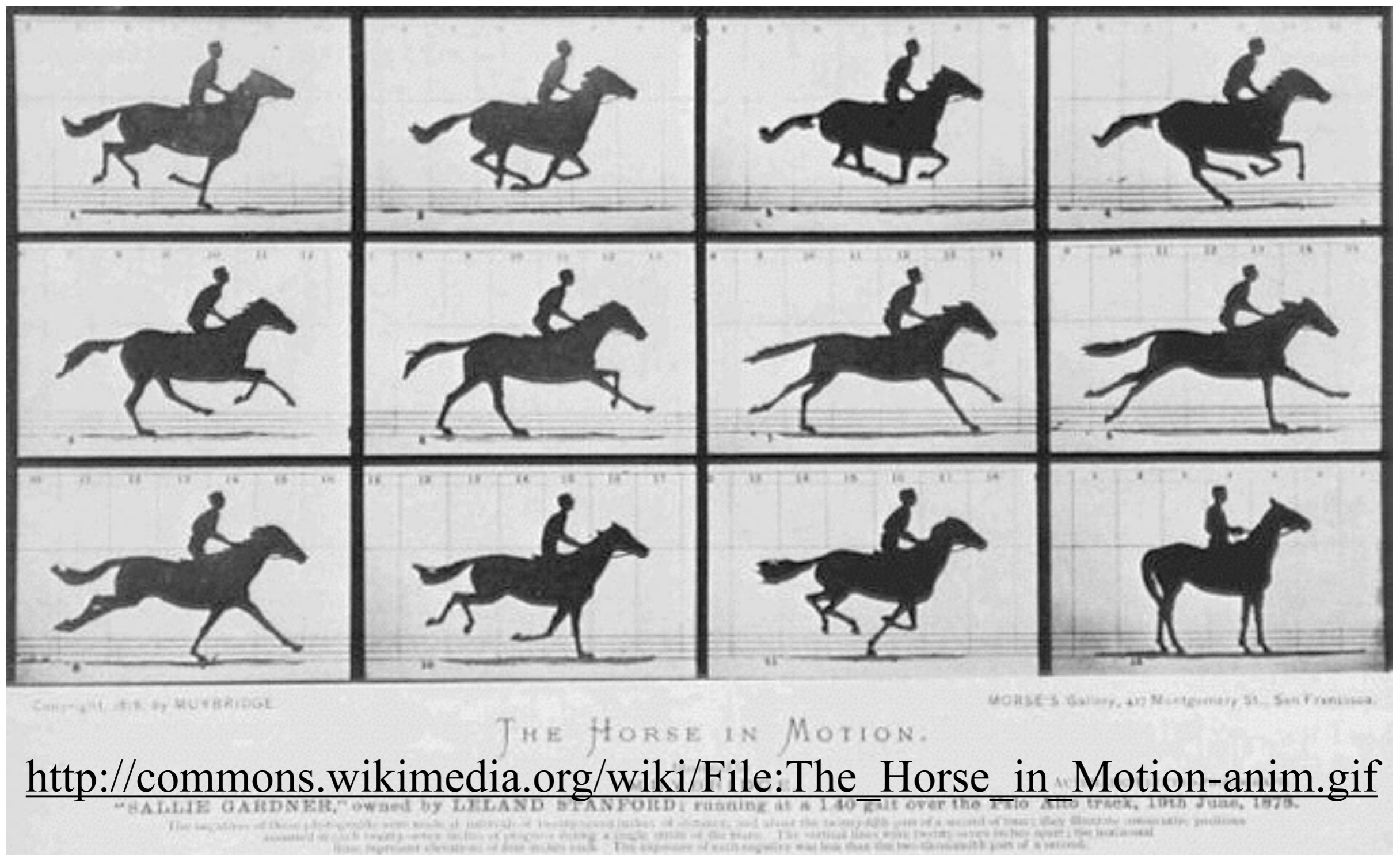
AUTOMATIC ELECTRO-PHOTOGRAPHY

"SALLIE GARDNER," owned by LELAND STANFORD; running at a 1.40 gait over the Palo Alto track, 19th June, 1878.

The negatives of these photographs were made at intervals of twenty-eighth inches of distance, and about the twenty-fifth part of a second of time; they illustrate consecutive positions assumed in each twenty-fourth inch of progress during a single stride of the horse. The vertical lines with twenty-seven inches apart; the horizontal lines represent elevations of four inches each. The exposure of each negative was less than the two-thousandth part of a second.

# Key Developments

- Max Fleischer invents rotoscoping (1921)

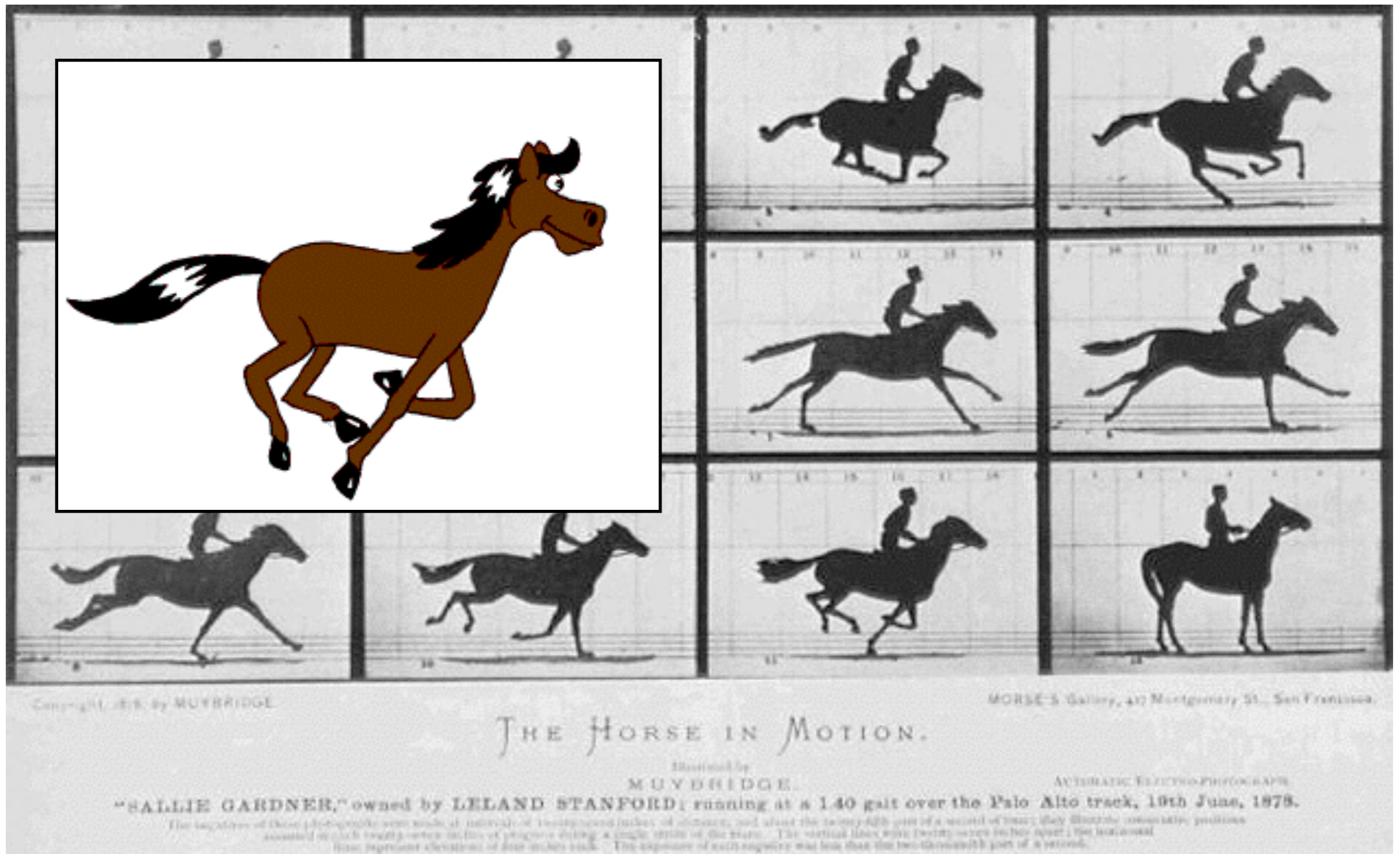






# Key Developments

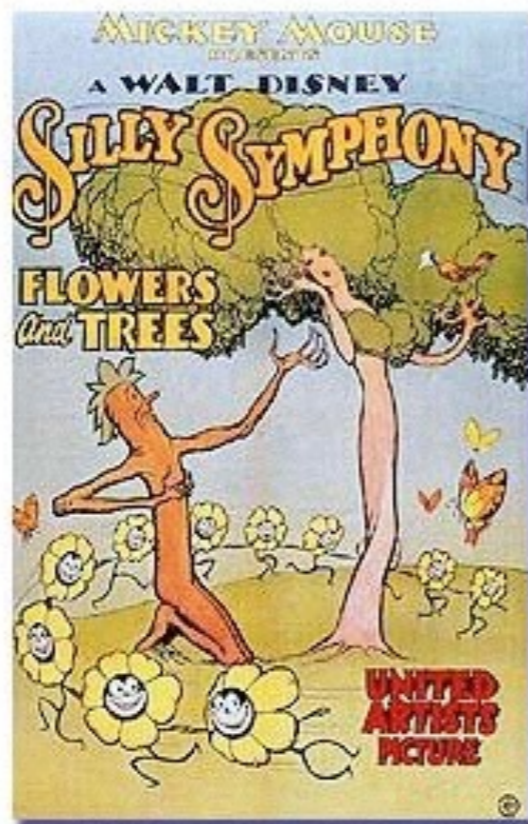
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# Key Developments

- “Flowers and Trees” (1932) uses color!
- “Snow White” (aka “Disney’s Folly”) released 1937



“Flowers and Trees”  
Walt Disney



“Snow White”  
Walt Disney

# Animation Uses

- Entertainment
- Education
- Propaganda

# Overview

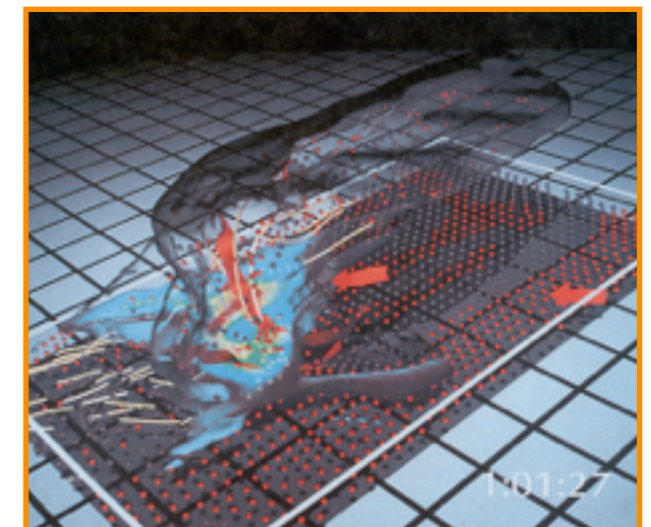
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- Computer animation

# Computer Animation

- What is animation?
  - Make objects change over time according to scripted actions
- What is simulation?
  - Predict how objects change over time according to physical laws



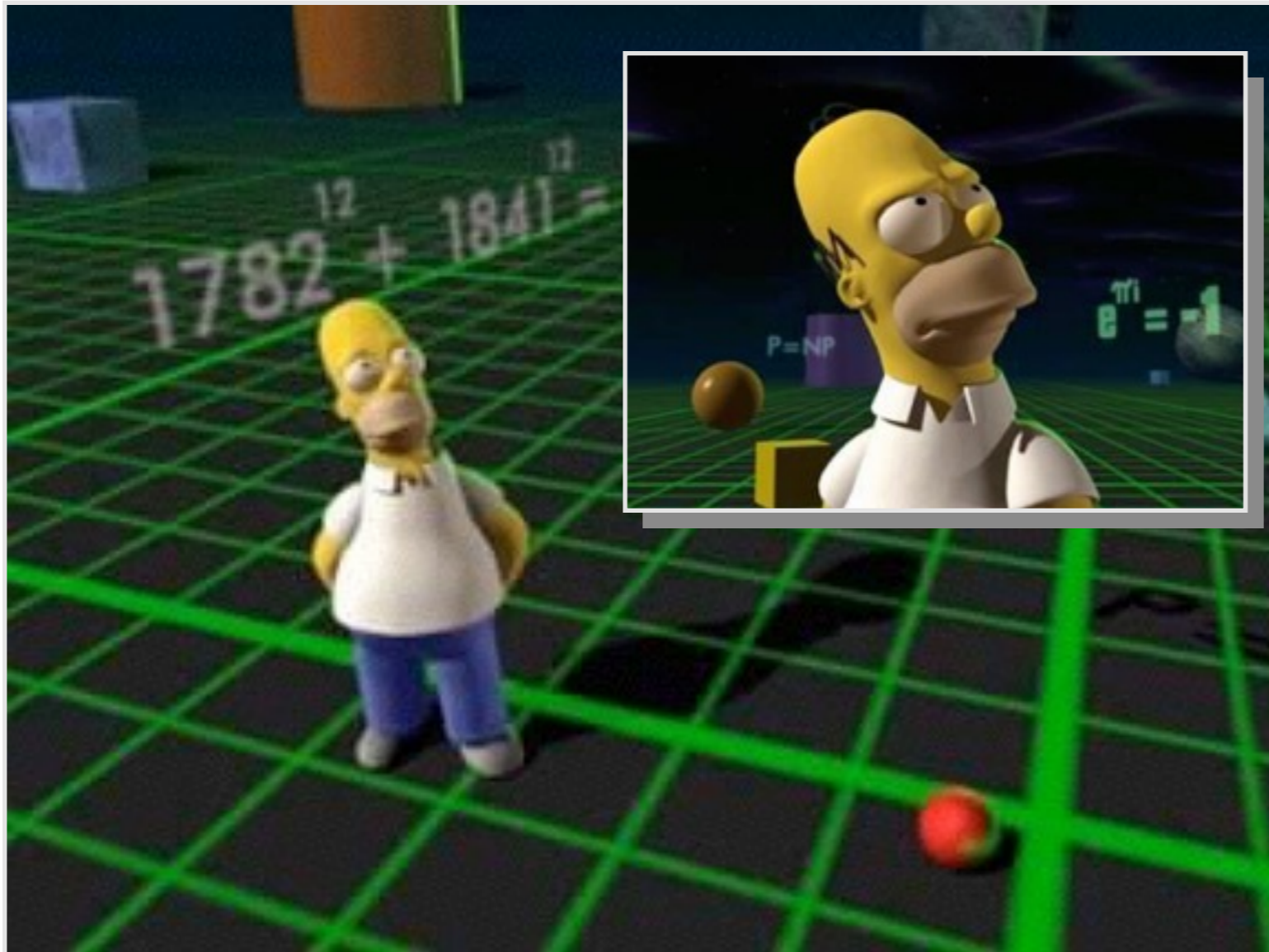
Pixar



University of Illinois



# 3-D and 2-D animation



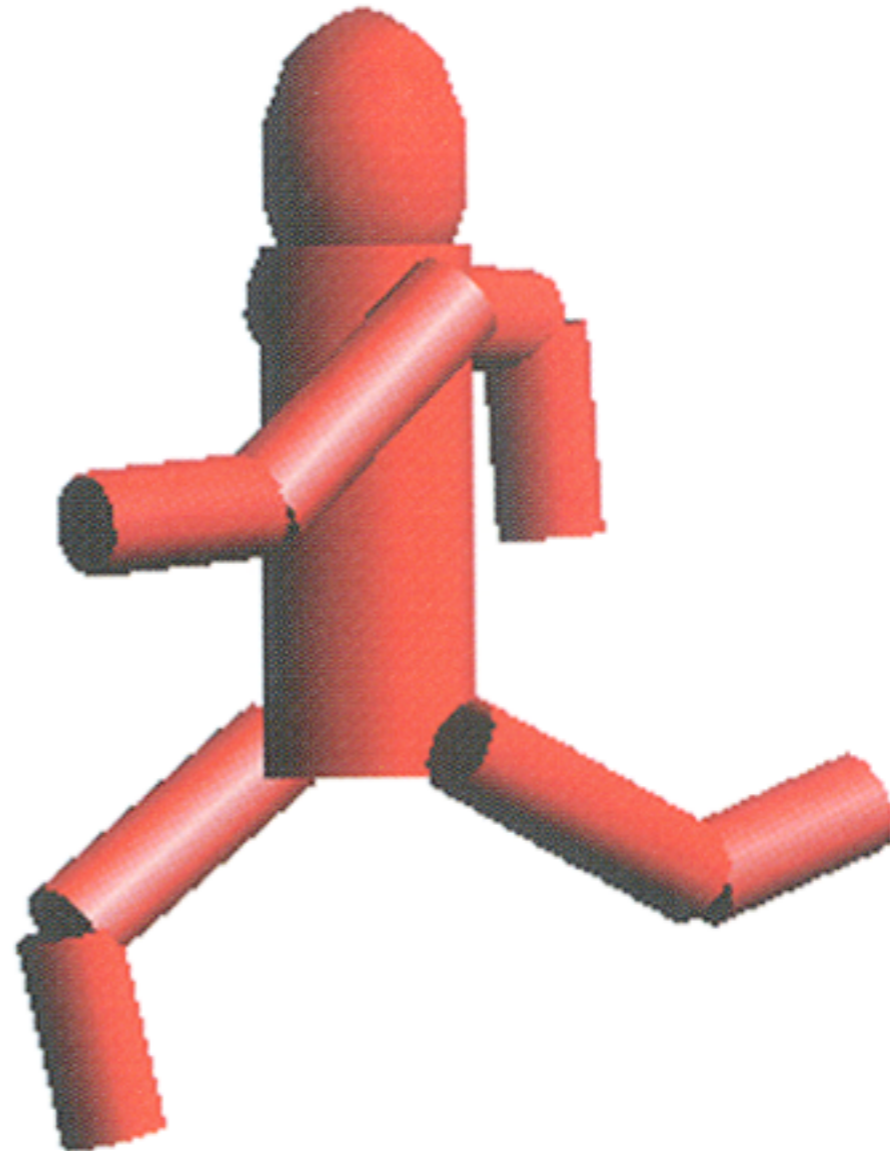
Homer 3-D



Homer 2-D

# Outline

- Principles of animation
- Keyframe animation
- Articulated figures



# Principles of Traditional Animation

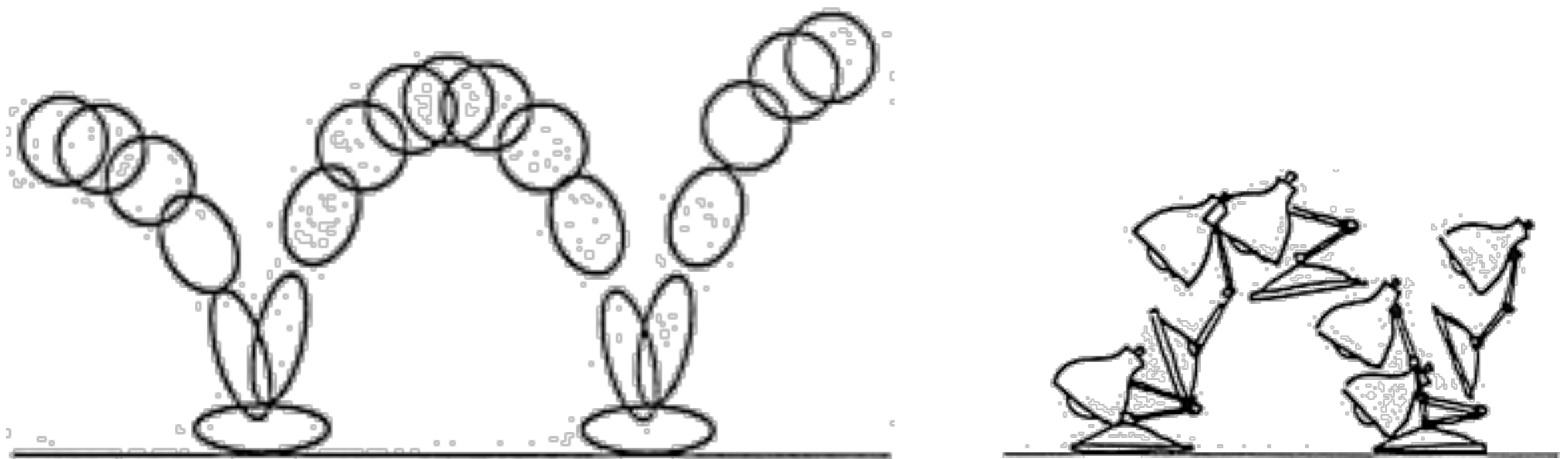
- Squash and Stretch
- Timing
- Anticipation
- Staging
- Follow Through and Overlapping Action
- Straight Ahead Action and Pose-to-Pose Action
- Slow In and Out
- Arcs
- Exaggeration
- Secondary action
- Appeal

Luxo Junior Short Film

# Principles of Traditional Animation

## Squash and Stretch

- Defining the rigidity and mass of an object by distorting its shape during an action.



# Principles of Traditional Animation

## Timing

- Spacing actions to define the weight and size of objects and the personality of characters.
  - Heavier objects accelerate slower
  - Lethargic characters move slower
  - Etc.

# Principles of Traditional Animation

## Anticipation

- The preparation for an action.
  - Muscle contraction prior to extension
  - Bending over to lift a heavy object
  - Luxo's dad responds to Luxo Jr. off screen before Luxo Jr. appears.



# Principles of Traditional Animation

## Staging

- Presenting an idea so that it is unmistakably clear.
  - Keeping the viewer's attention focused on a specific part of the scene.
  - Luxo Jr. moves faster than his dad, and so we focus on him.

# Principles of Traditional Animation

## Follow Through and Overlapping Action

- The termination of an action and establishing its relationship to the next action.
  - Loose clothing will “drag” and continue moving after the character has stopped moving.
  - The way in which an object slows down indicates its weight/mood.

# Principles of Traditional Animation

## Straight Ahead Action and Pose-to-Pose Action

- The two contrasting approaches to the creation of movement.
  - **Straight Ahead Action:**
    - » Action is drawn from the first frame through to the last one.
    - » Wild, scrambling actions where spontaneity is important.
  - **Pose-to-Pose Action:**
    - » Poses are pre-conceived and animator fills in the in-betweens.
    - » Good acting, where the poses and timing are all important.

# Principles of Traditional Animation

## Slow In and Out

- The spacing of in-between frames to achieve subtlety of timing and movements.

# Principles of Traditional Animation

## Arcs

- The visual path of action for natural movement.
  - Make animation much smoother and less stiff than a straight line for the path of action



# Principles of Traditional Animation

## Exaggeration

- Accentuating the essence of an idea via the design and the action.

# Principles of Traditional Animation

## Secondary Action

- The Action of an object resulting from another action.
  - The rippling of Luxo Jr.'s cord as he bounces around the scene.

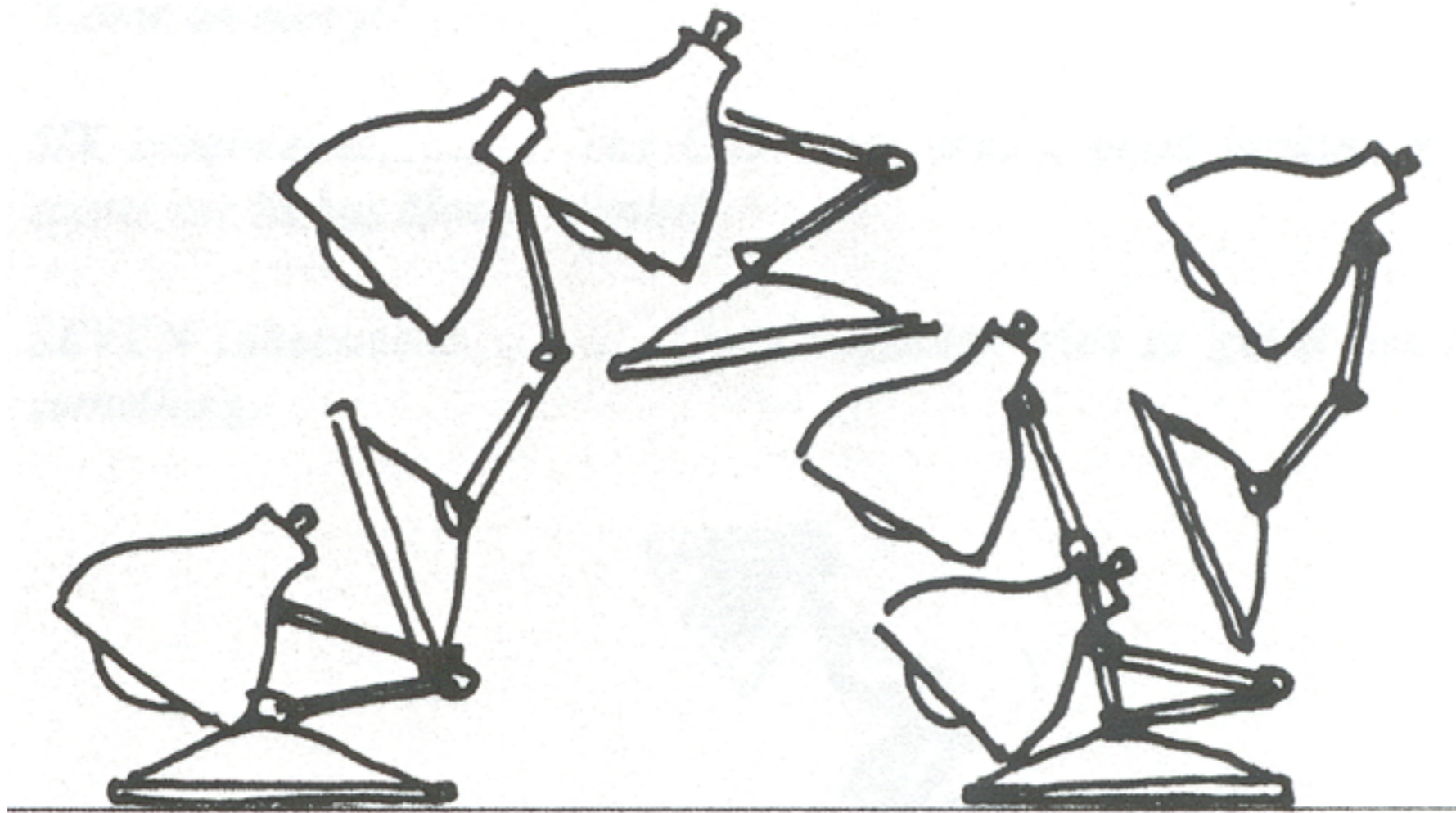
# Principles of Traditional Animation

## Appeal

- Creating a design or an action that the audience enjoys watching.
  - Charm
  - Pleasing design
  - Simplicity
  - Communication
  - Magnetism
  - Etc.

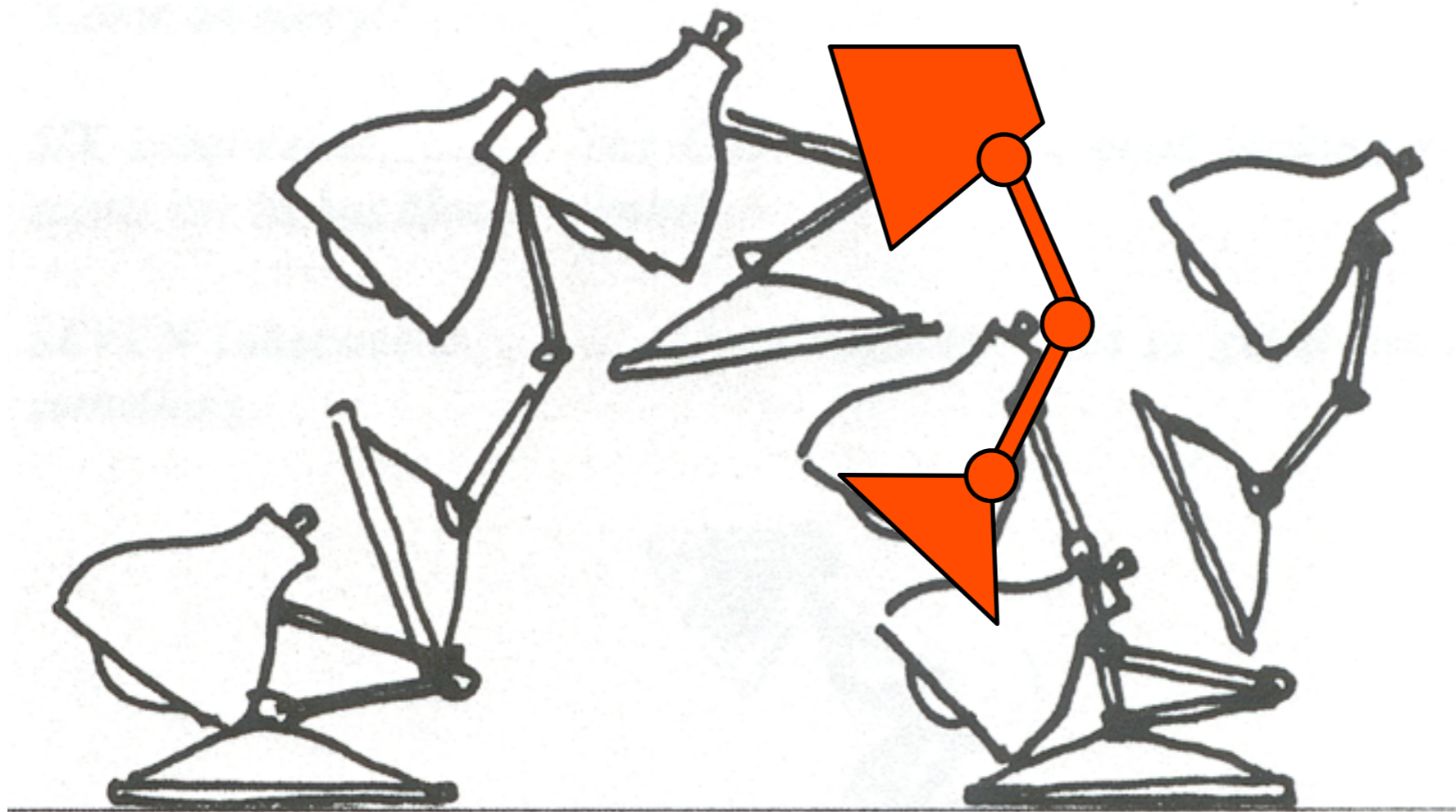
# Keyframe Animation

- Define character poses at specific time steps called “keyframes”



# Keyframe Animation

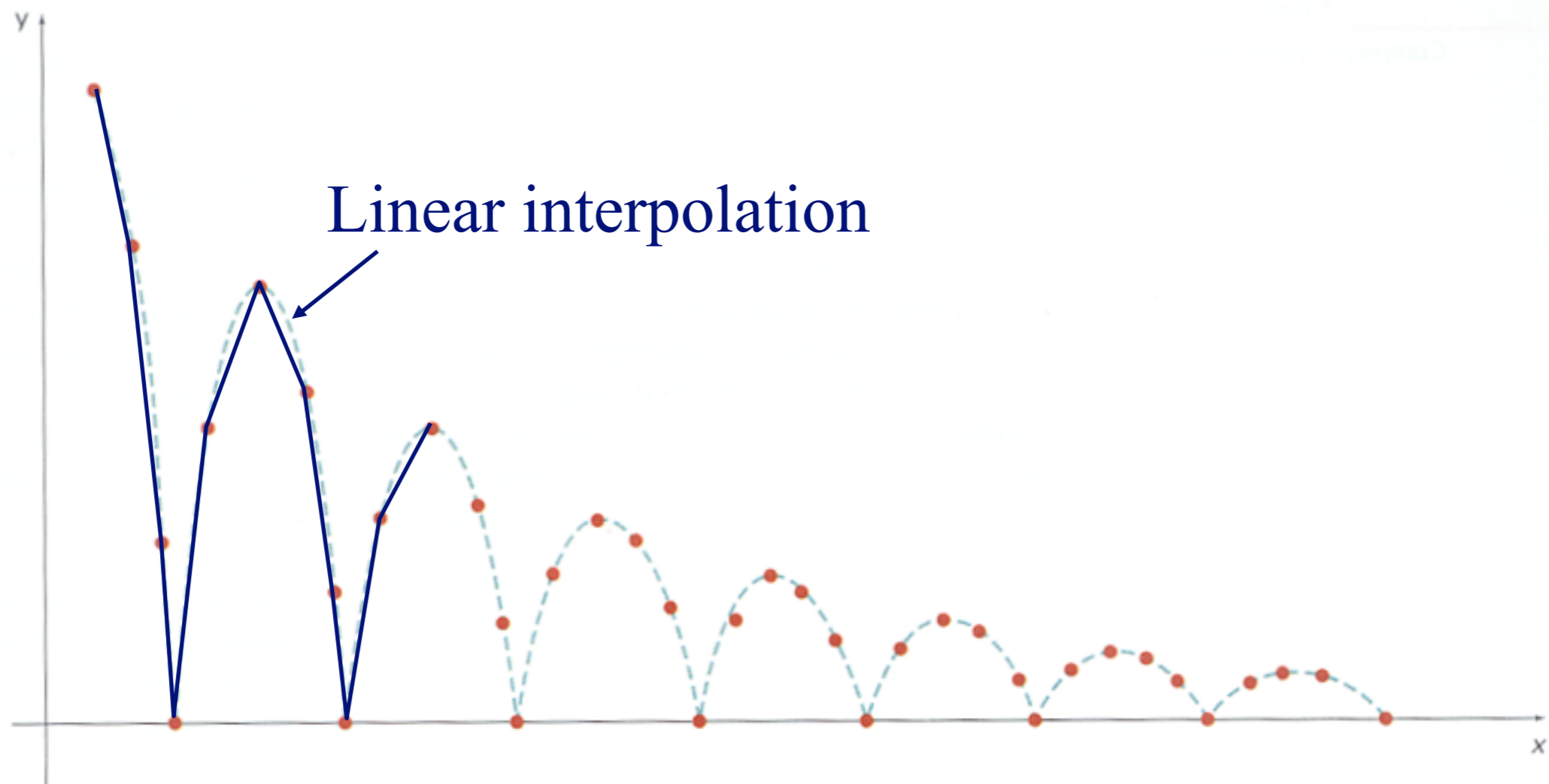
- Interpolate variables describing keyframes to determine poses for character “in-between”





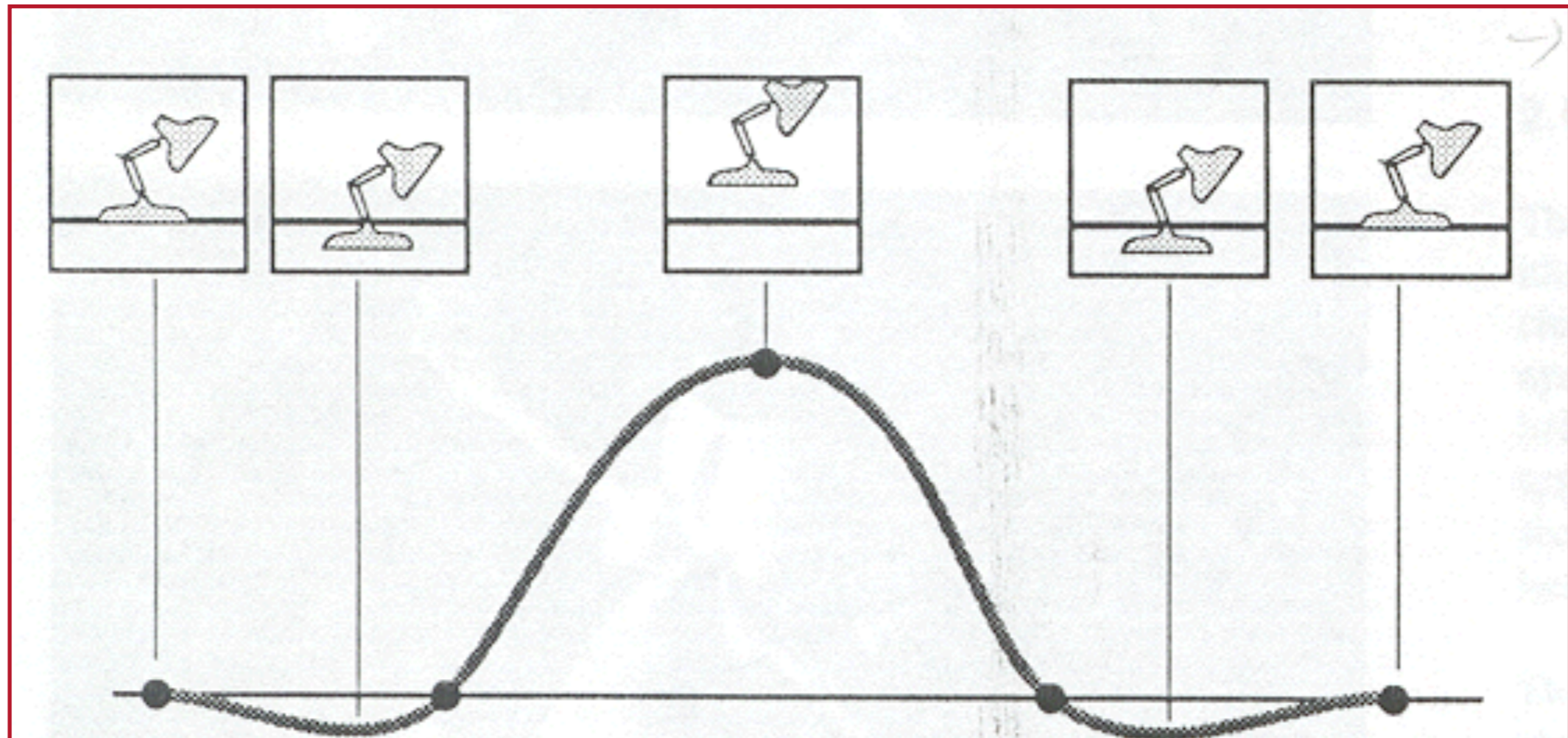
# Keyframe Animation

- Inbetweening:
  - Linear interpolation - usually not enough continuity



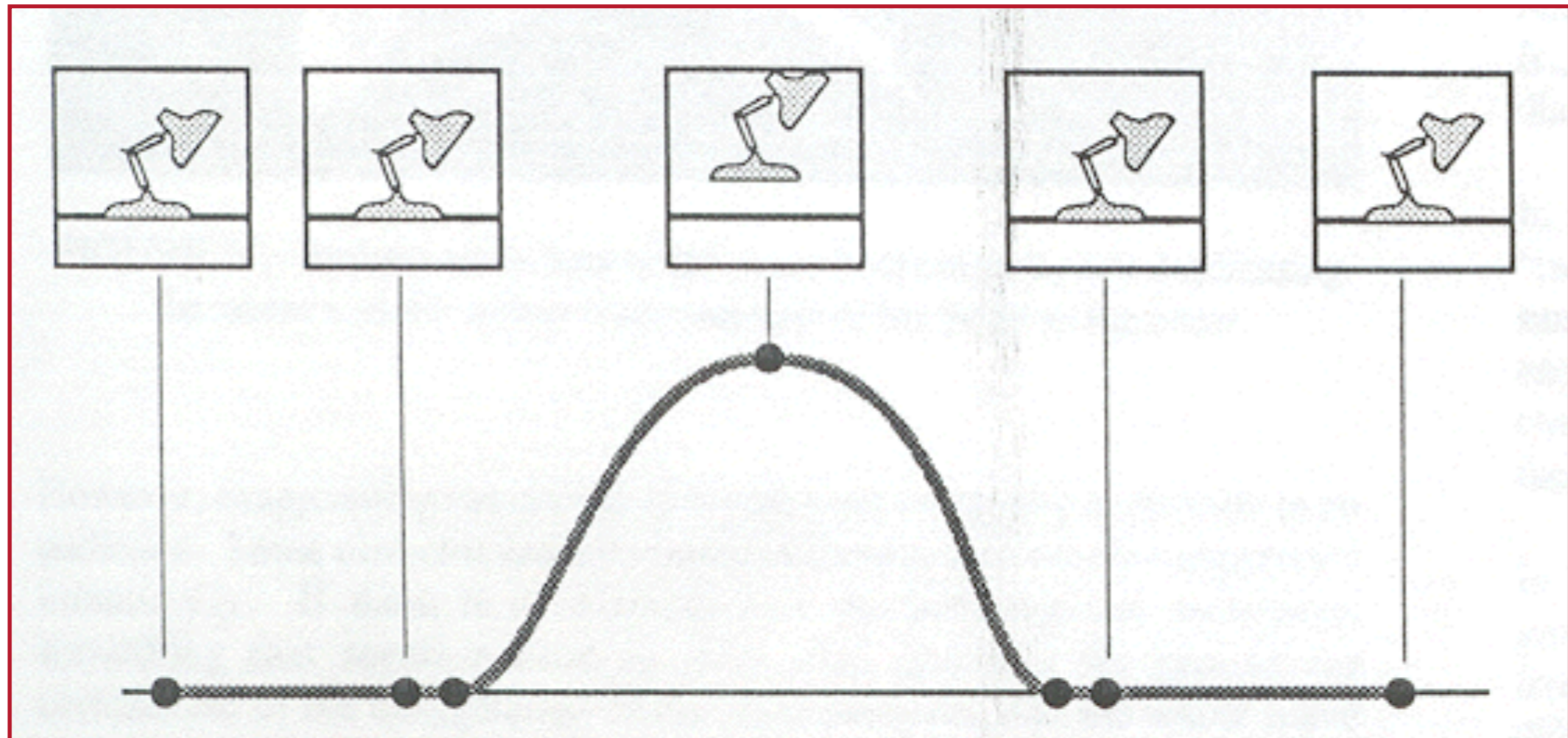
# Keyframe Animation

- Inbetweening:
  - Cubic spline interpolation - maybe good enough
    - » May not follow physical laws



# Keyframe Animation

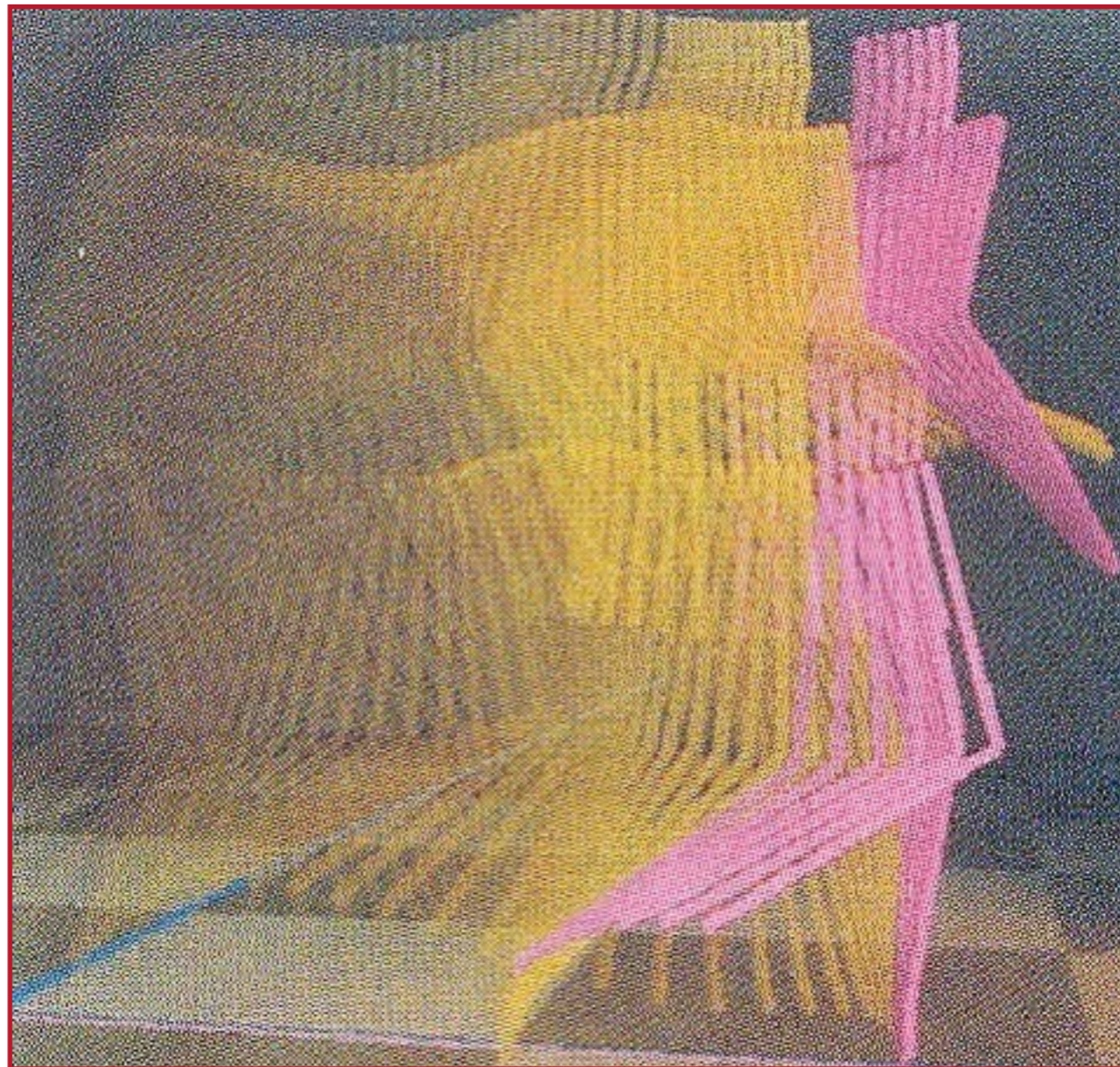
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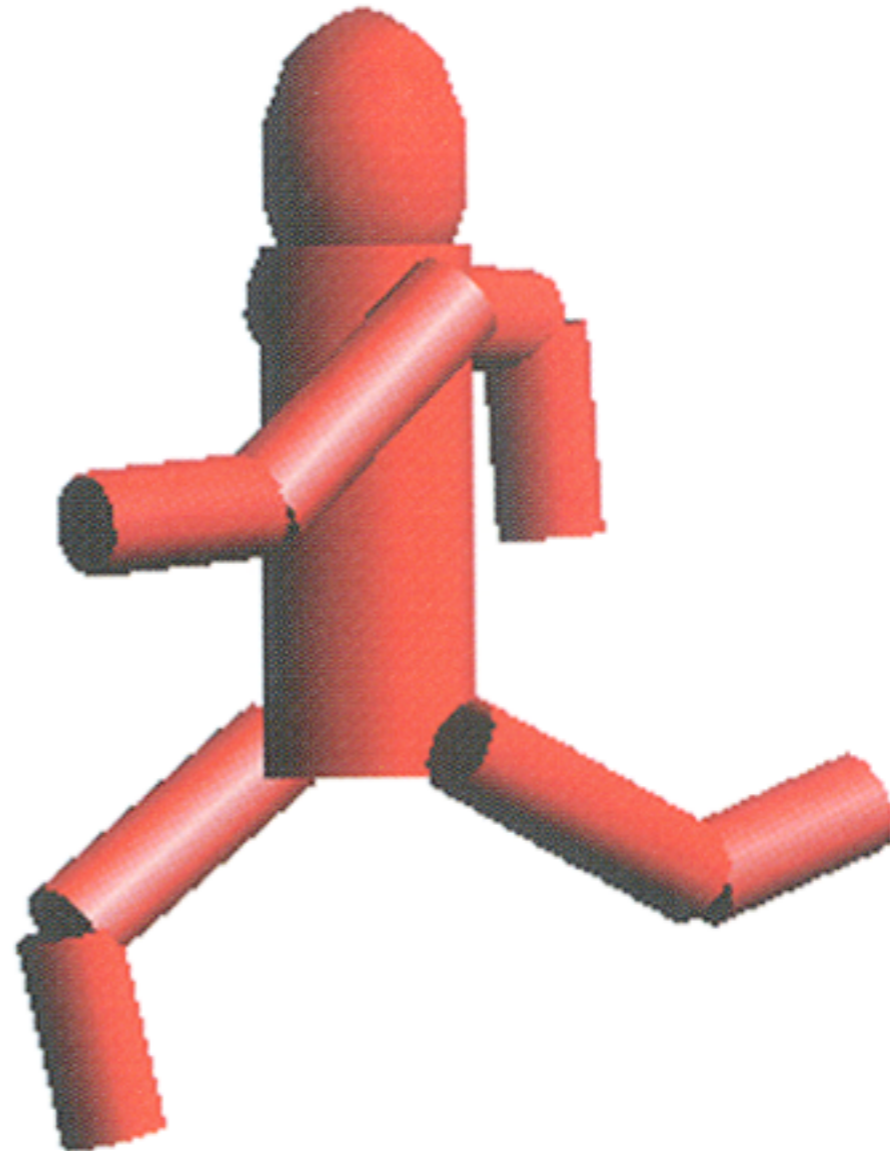
# Keyframe Animation

- Inbetweening:
  - Kinematics or dynamics



# Outline

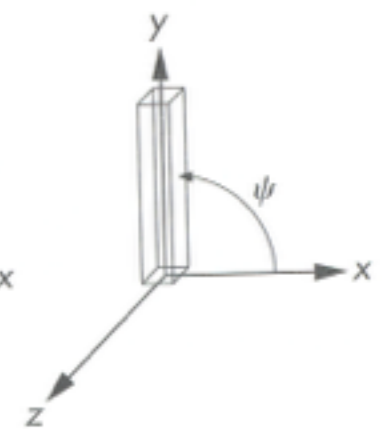
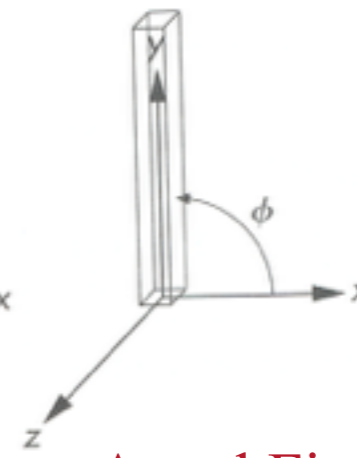
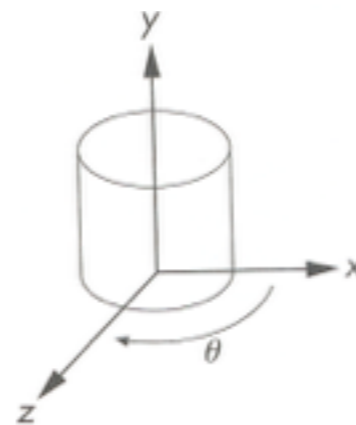
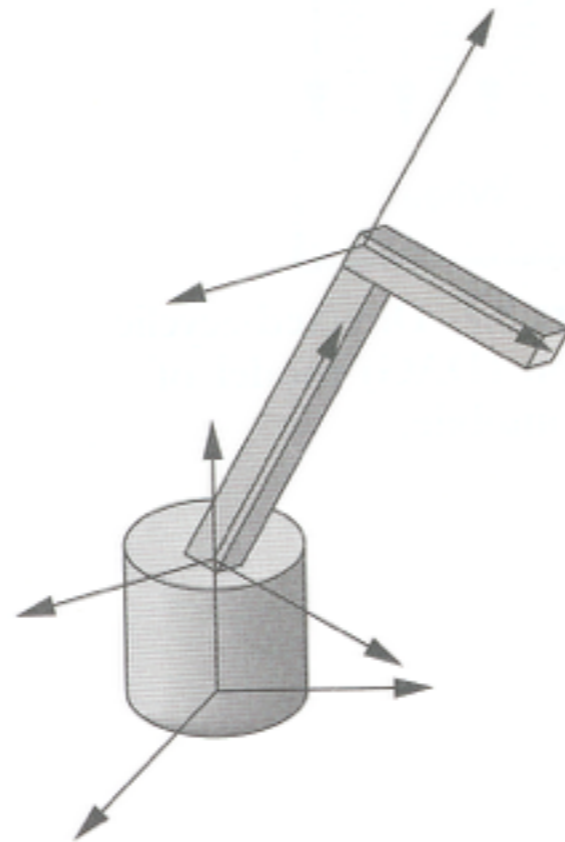
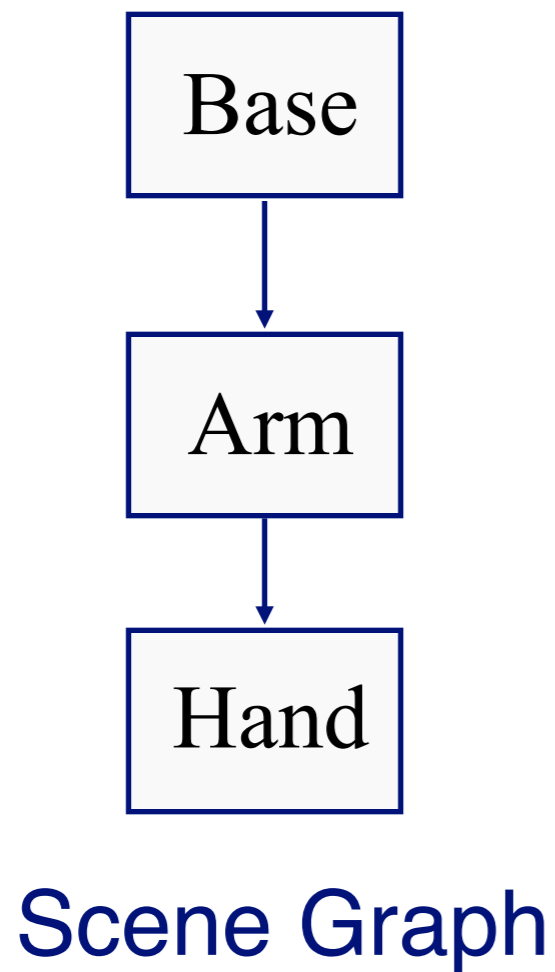
- Principles of animation
- Keyframe animation
- Articulated figures





# Articulated Figures

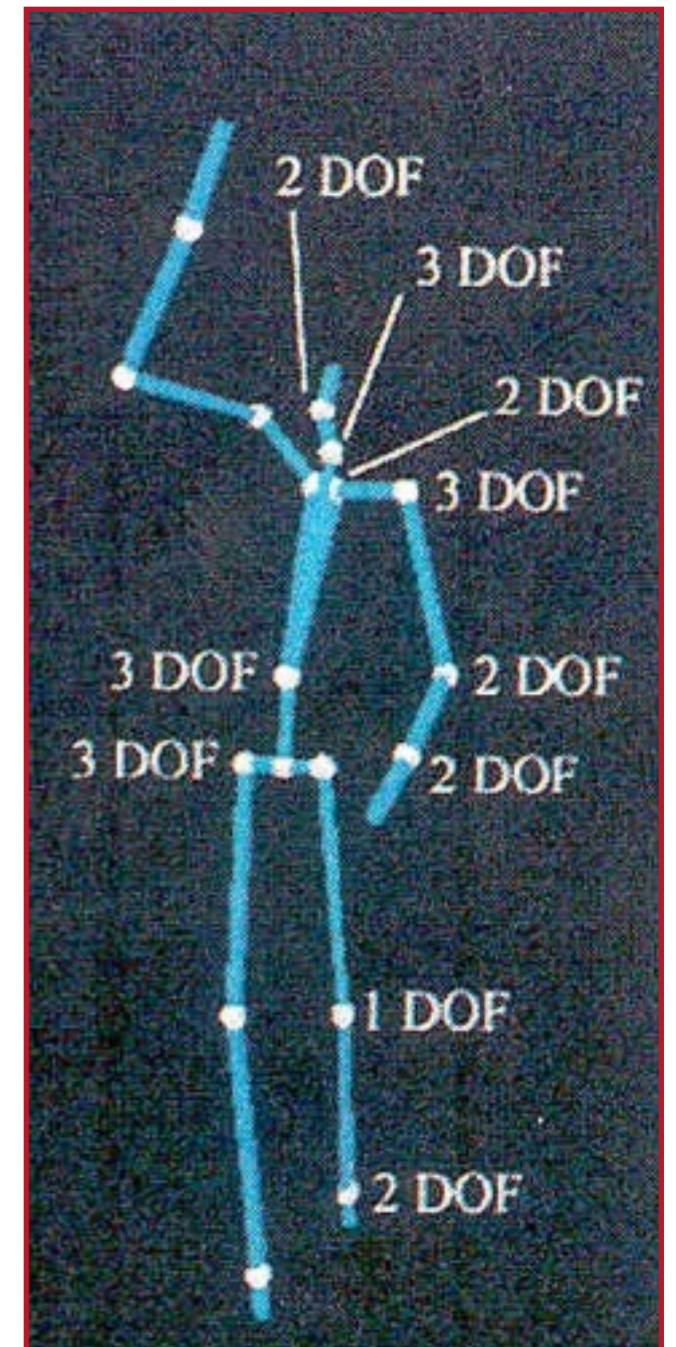
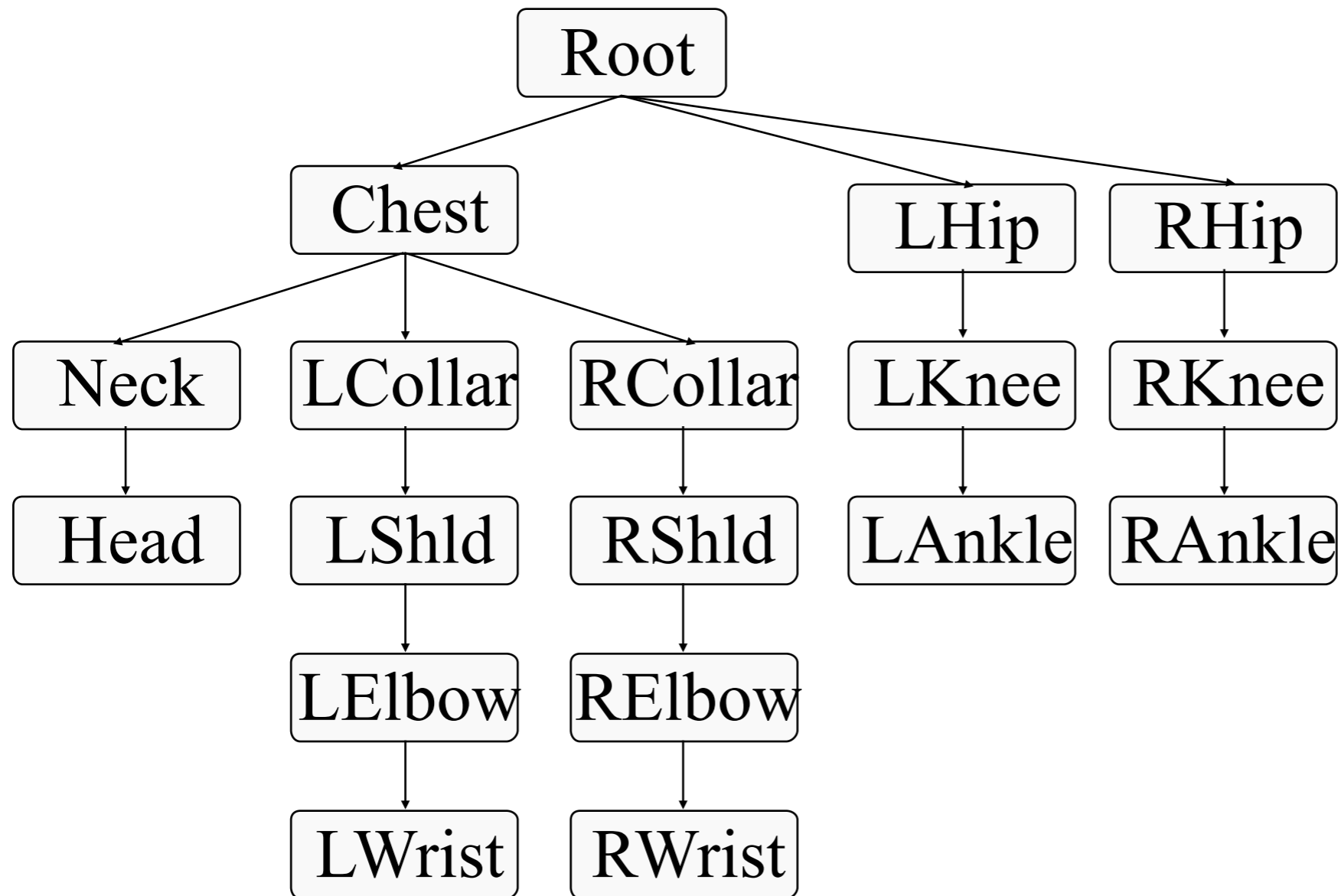
- Character poses described by set of rigid bodies connected by “joints”



Angel Figures 8.8 & 8.9

# Articulated Figures

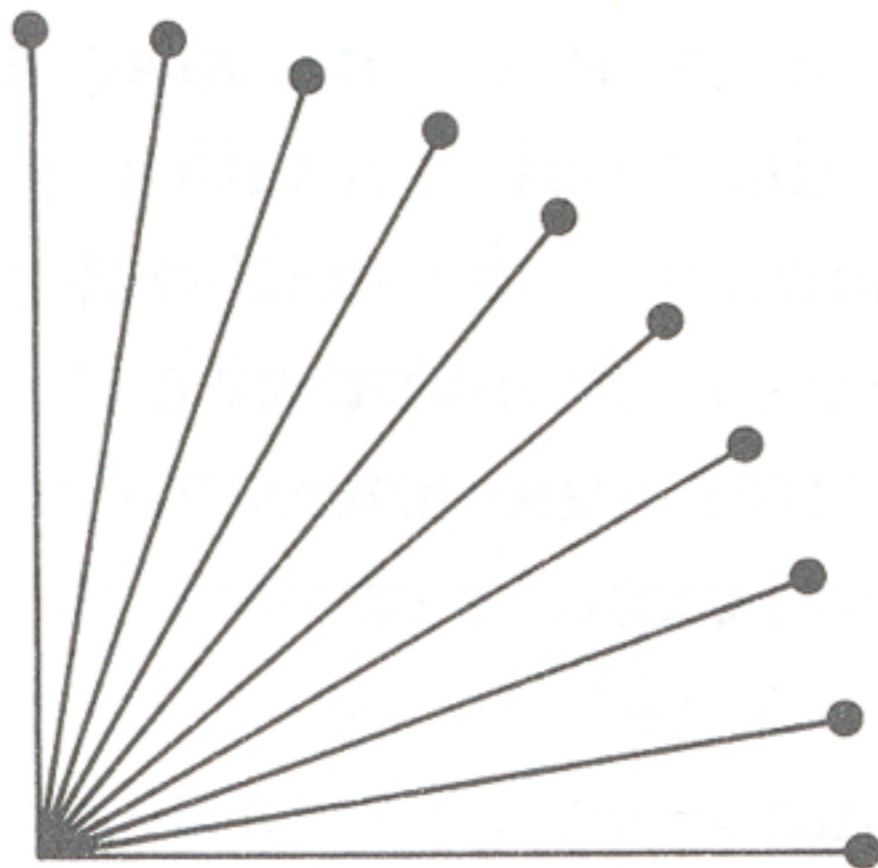
- Well-suited for humanoid characters



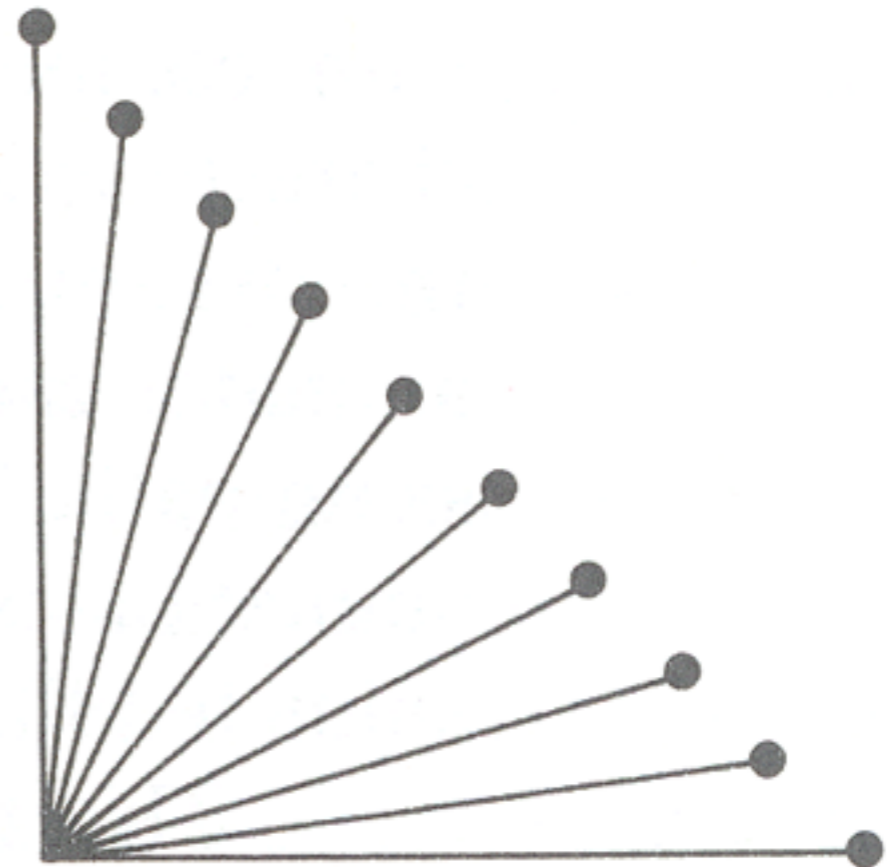
Rose et al. '96

# Articulated Figures

- Inbetweening
  - Interpolate angles, not positions, between keyframes



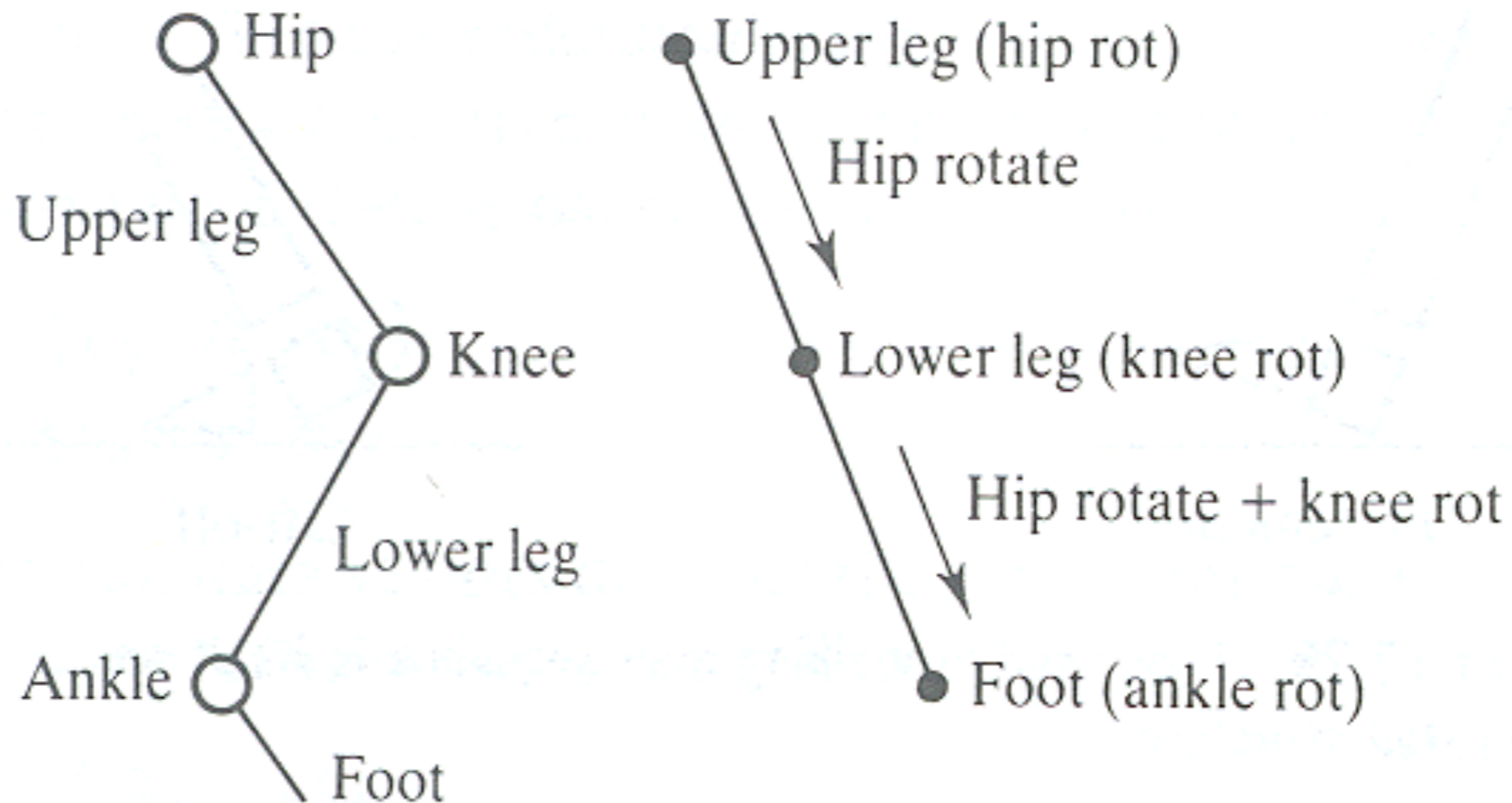
Good arm



Bad arm

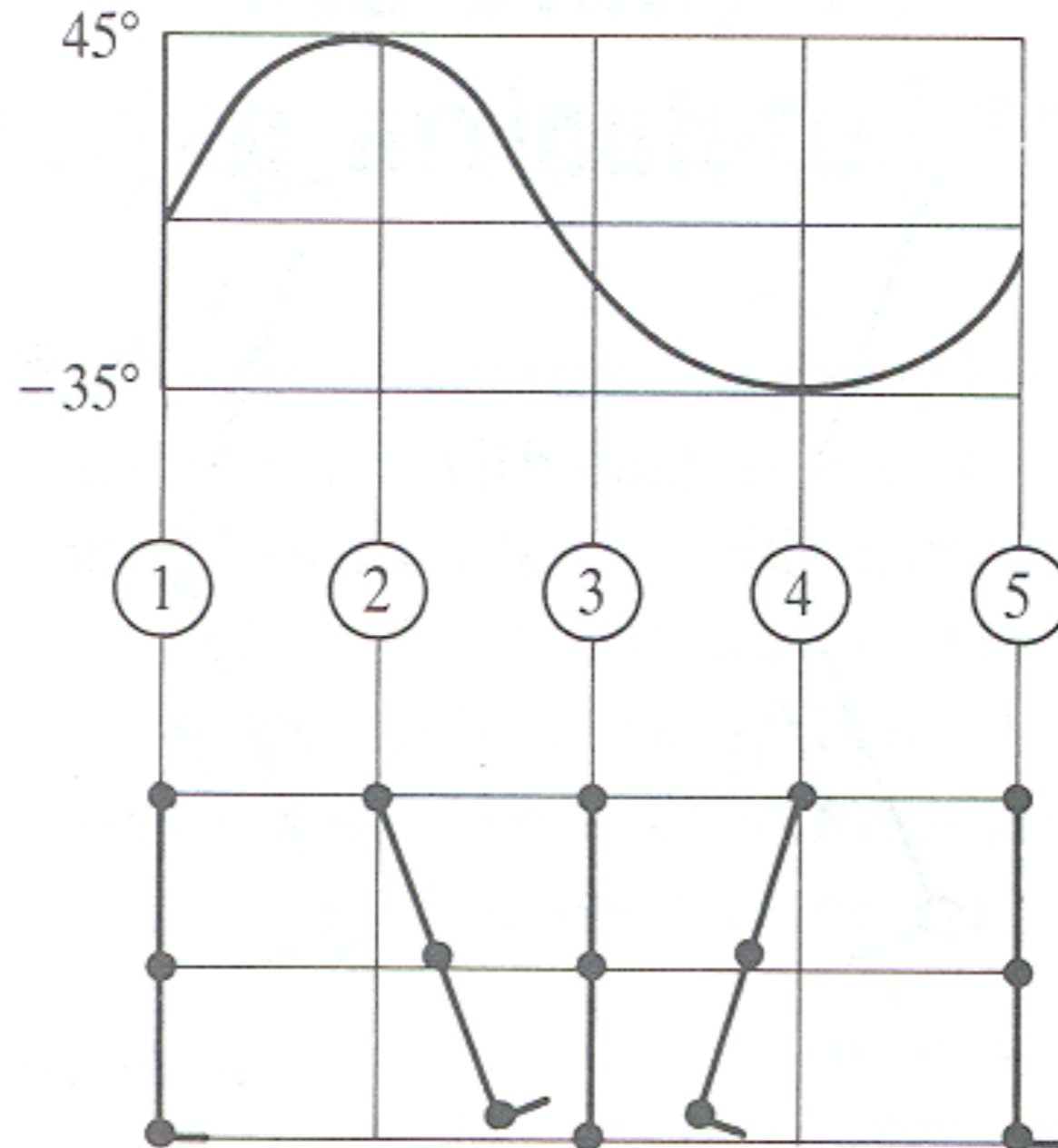
# Example: Walk Cycle

- Articulated figure:



# Example: Walk Cycle

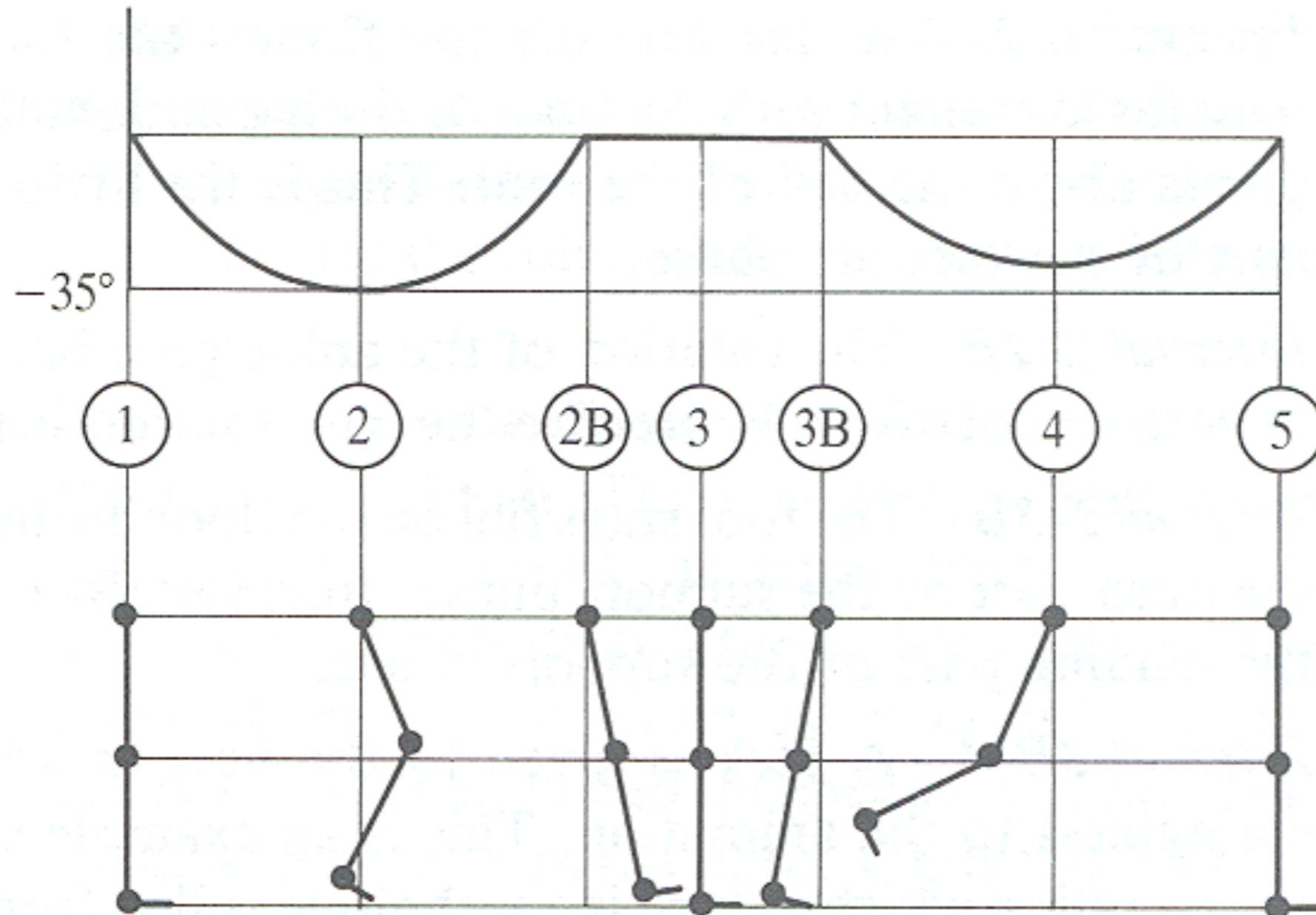
- Hip joint orientation:





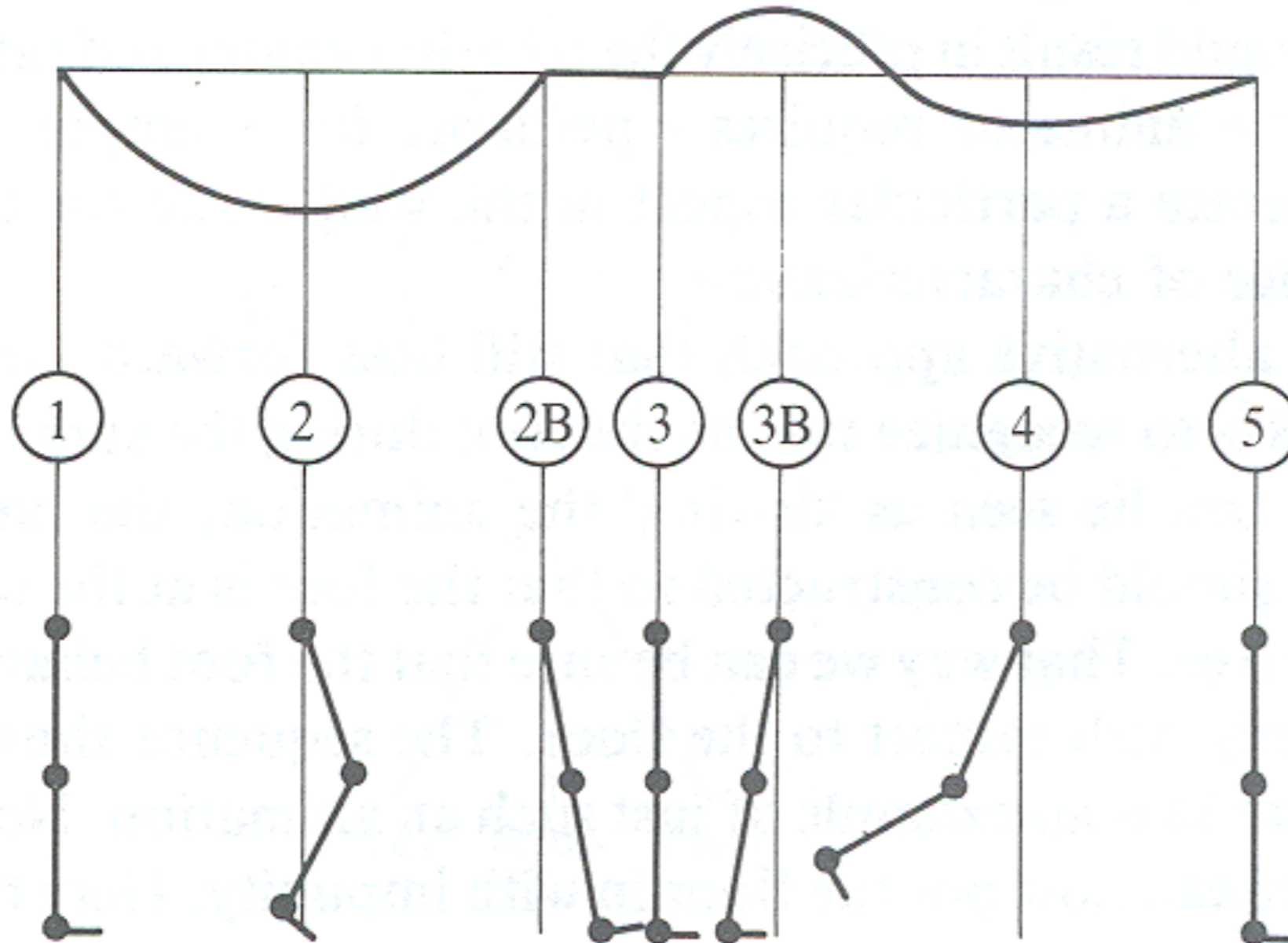
# Example: Walk Cycle

- Knee joint orientation:

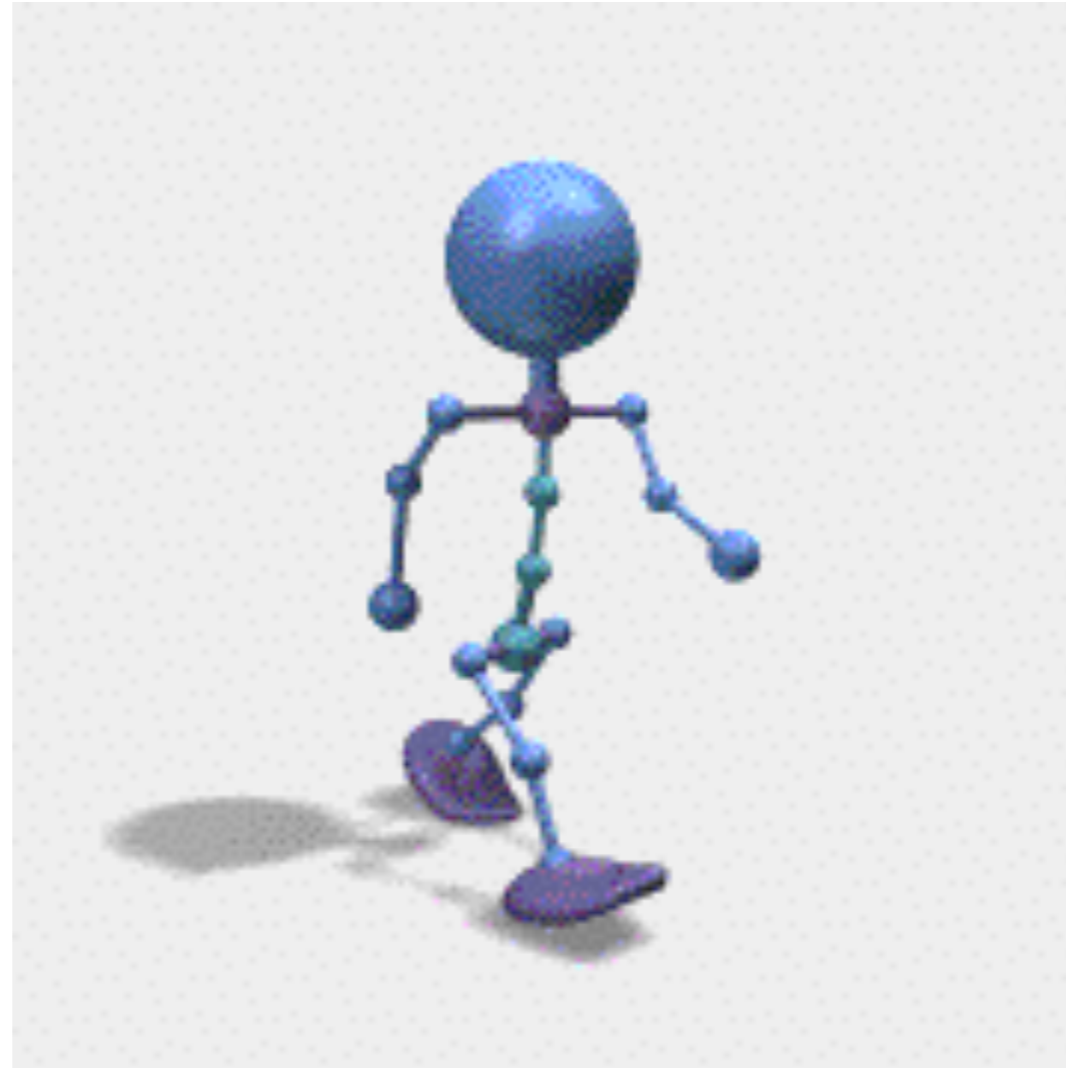


# Example: Walk Cycle

- Ankle joint orientation:



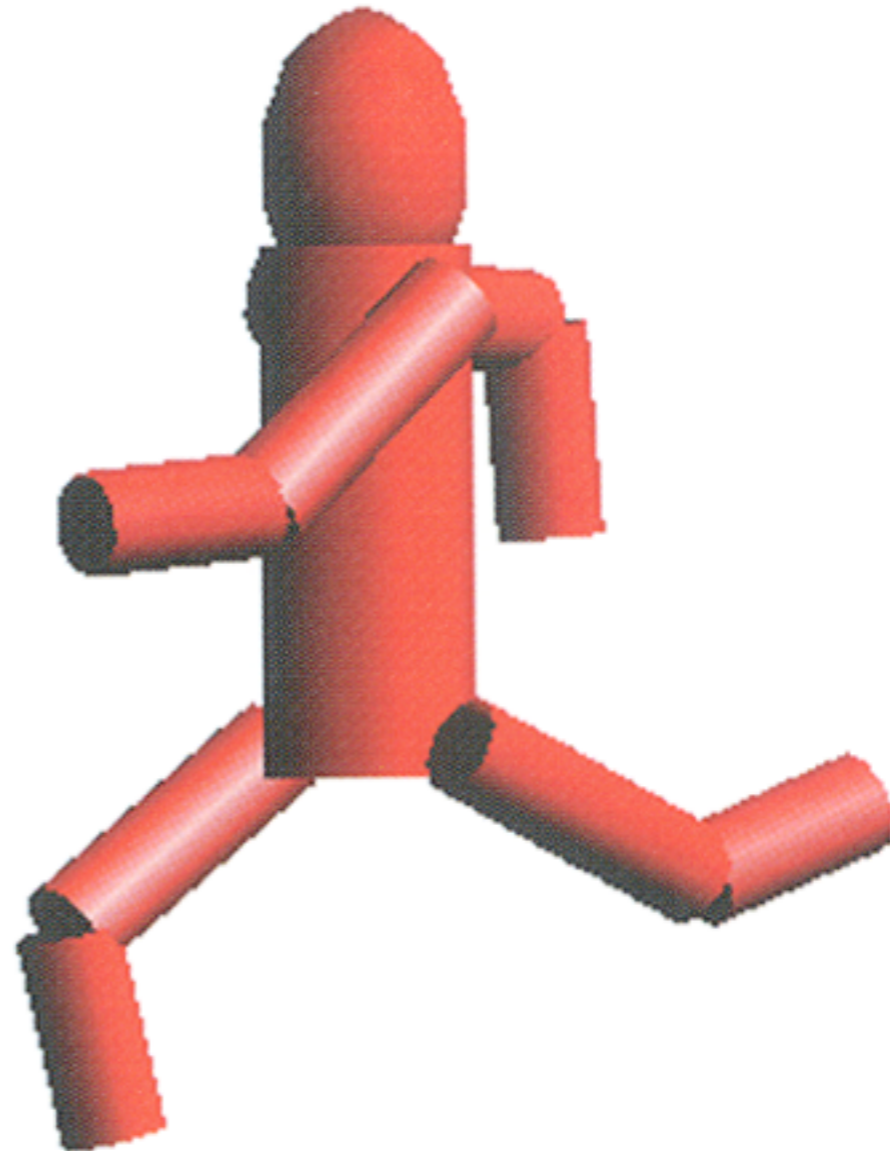
# Example: Walk Cycle



<https://www.youtube.com/watch?v=k86w0zIzY54>

# Outline

- Principles of animation
- Keyframe animation
- Articulated figures



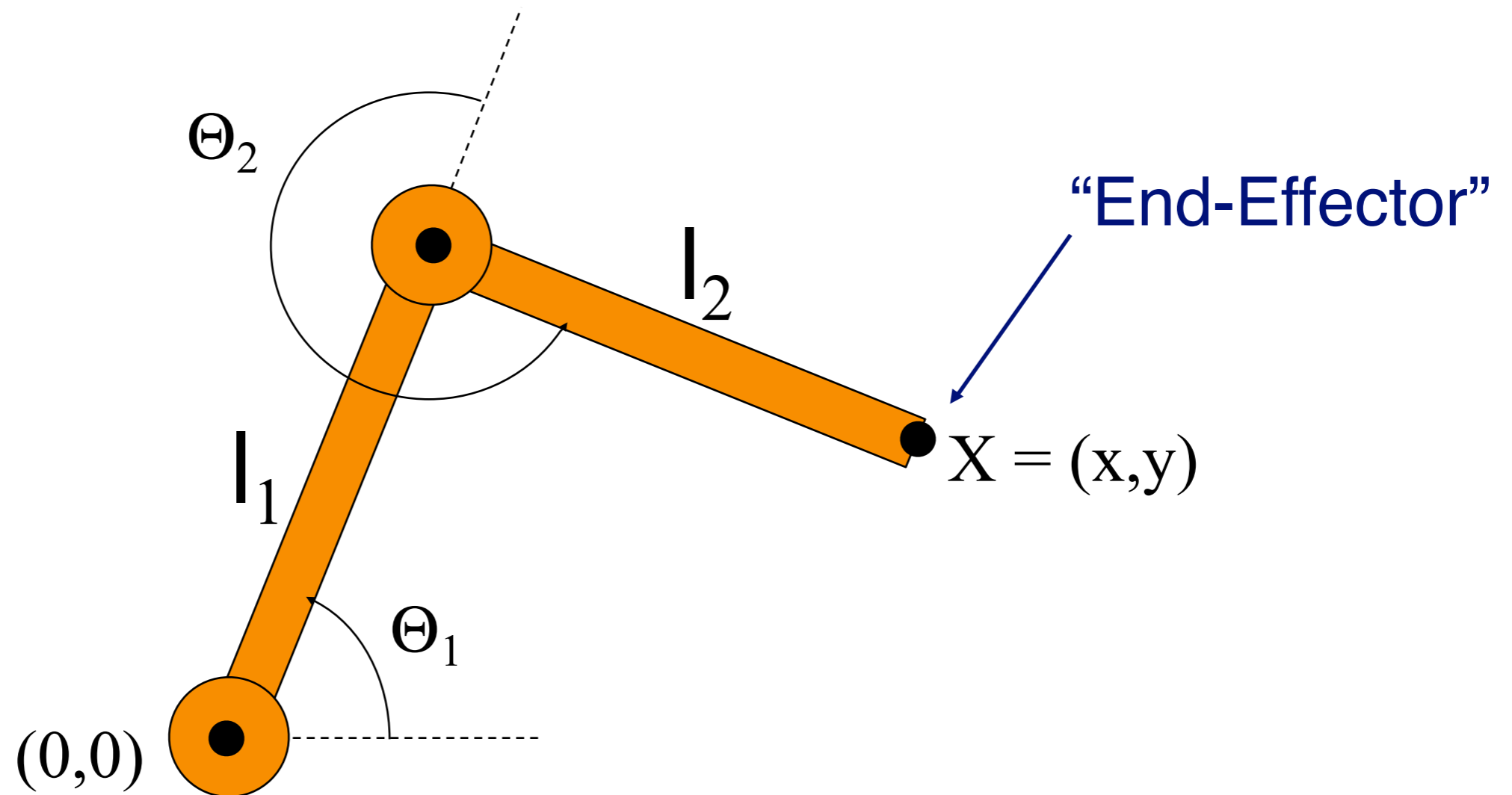
# Kinematics and Dynamics

- Kinematics
  - Considers only motion
  - Determined by positions, velocities, accelerations
- Dynamics
  - Considers underlying forces
  - Compute motion from initial conditions and physics



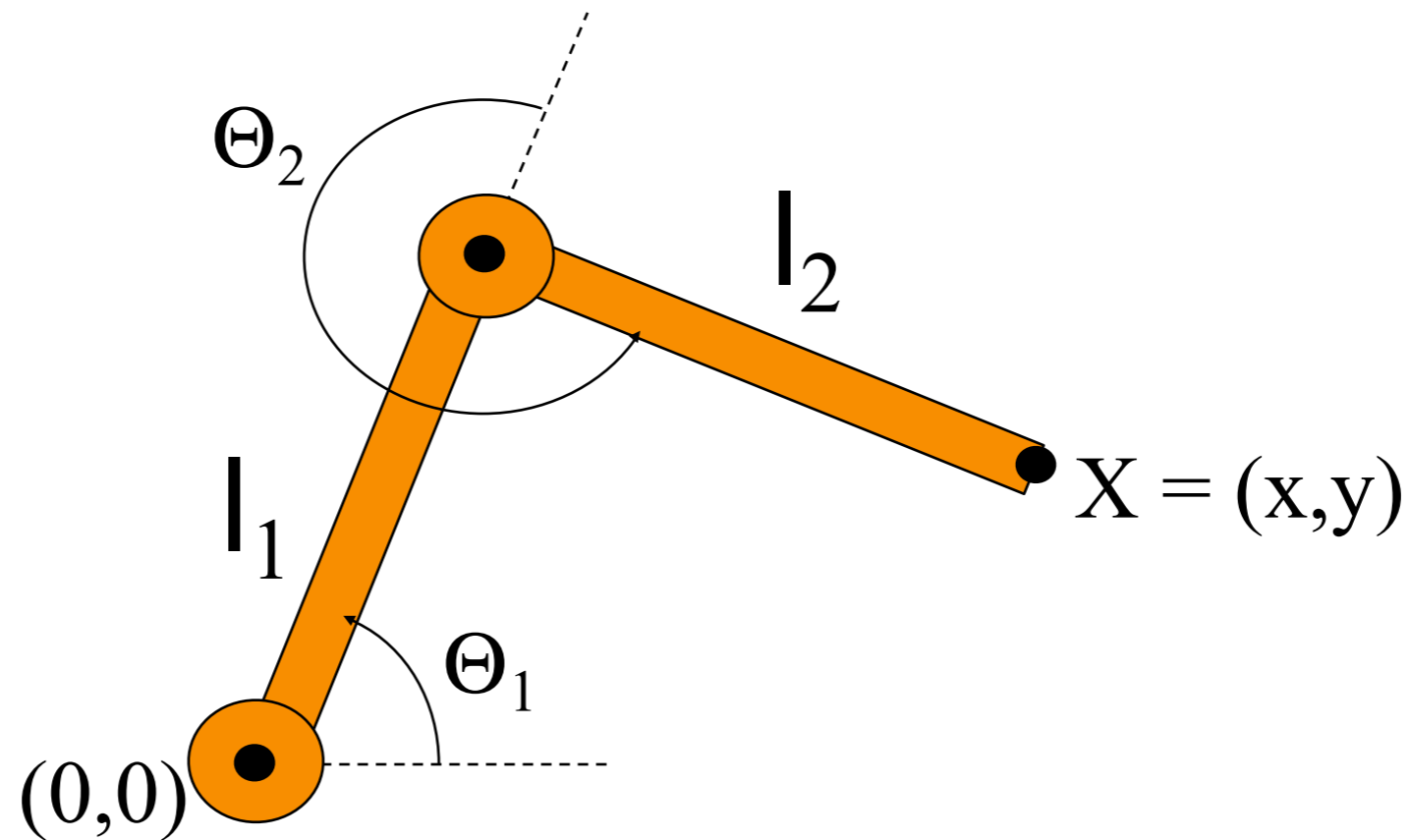
# Example: 2-Link Structure

- Two links connected by rotational joints



# Forward Kinematics

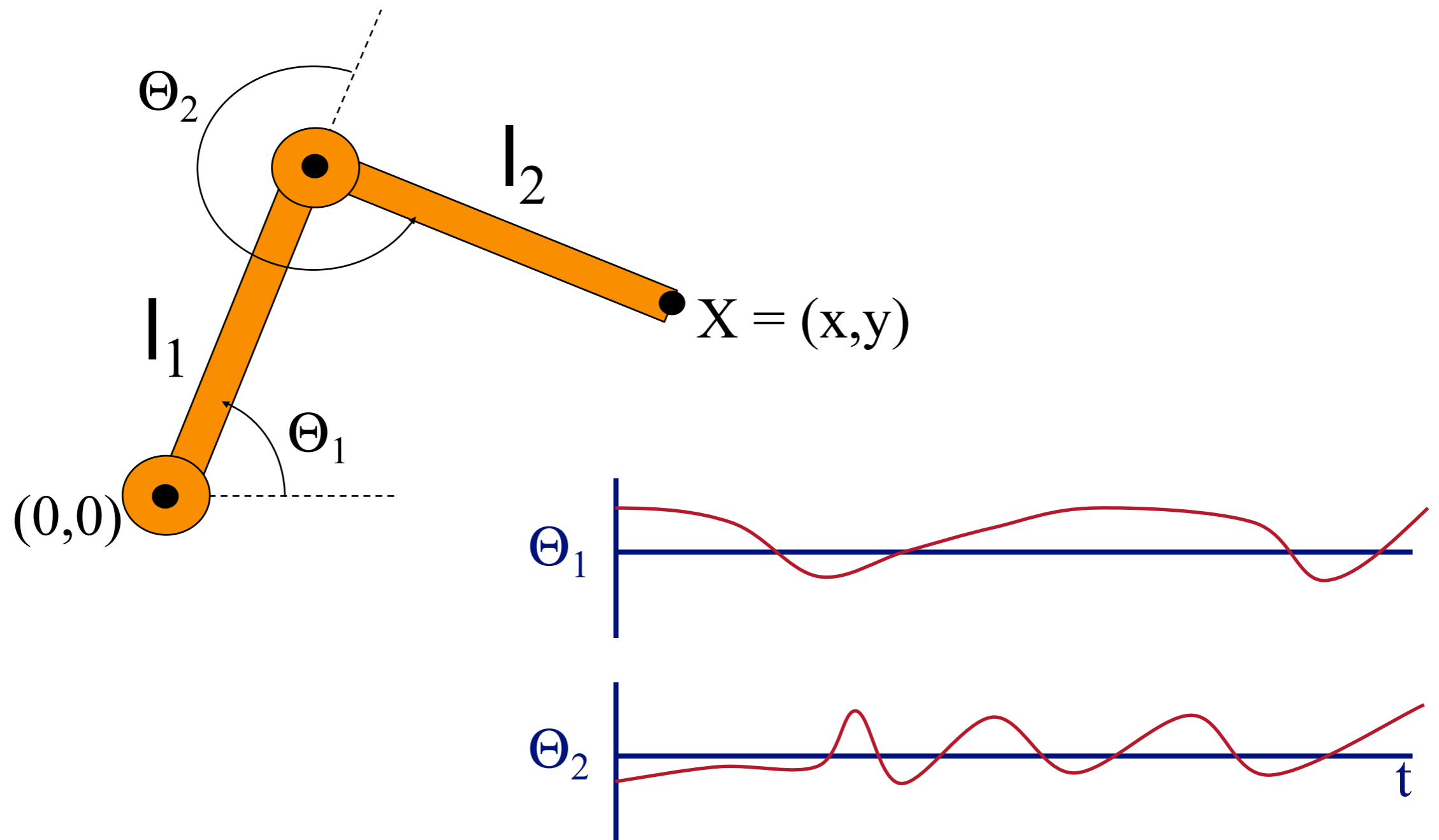
- Animator specifies joint angles:  $\Theta_1$  and  $\Theta_2$
- Computer finds positions of end-effector:  $X$



$$X = (l_1 \cos \Theta_1 + l_2 \cos(\Theta_1 + \Theta_2), l_1 \sin \Theta_1 + l_2 \sin(\Theta_1 + \Theta_2))$$

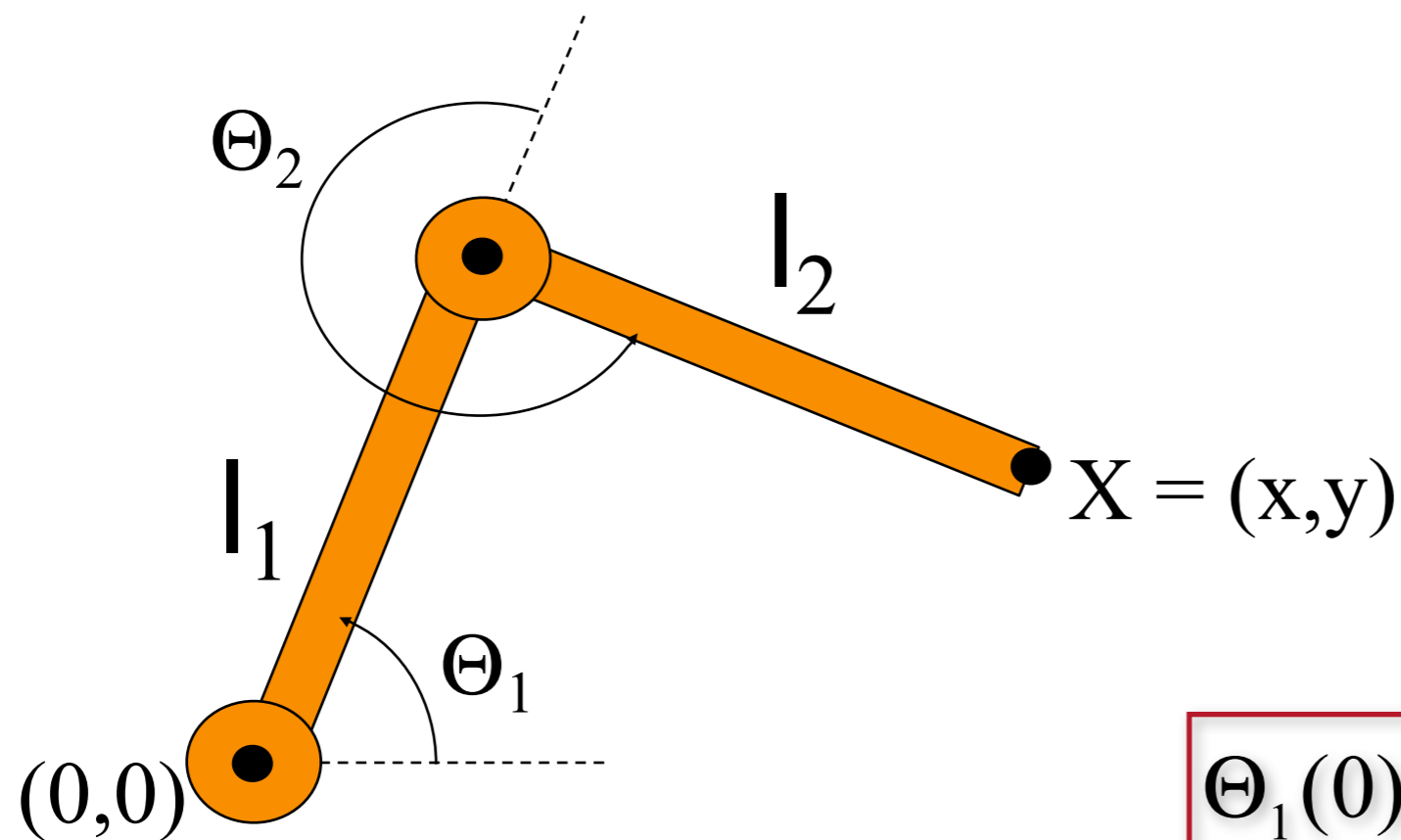
# Forward Kinematics

- Joint motions can be specified by spline curves



# Forward Kinematics

- Joint motions can be specified by initial conditions and velocities



$$\Theta_1(0) = 60^\circ$$

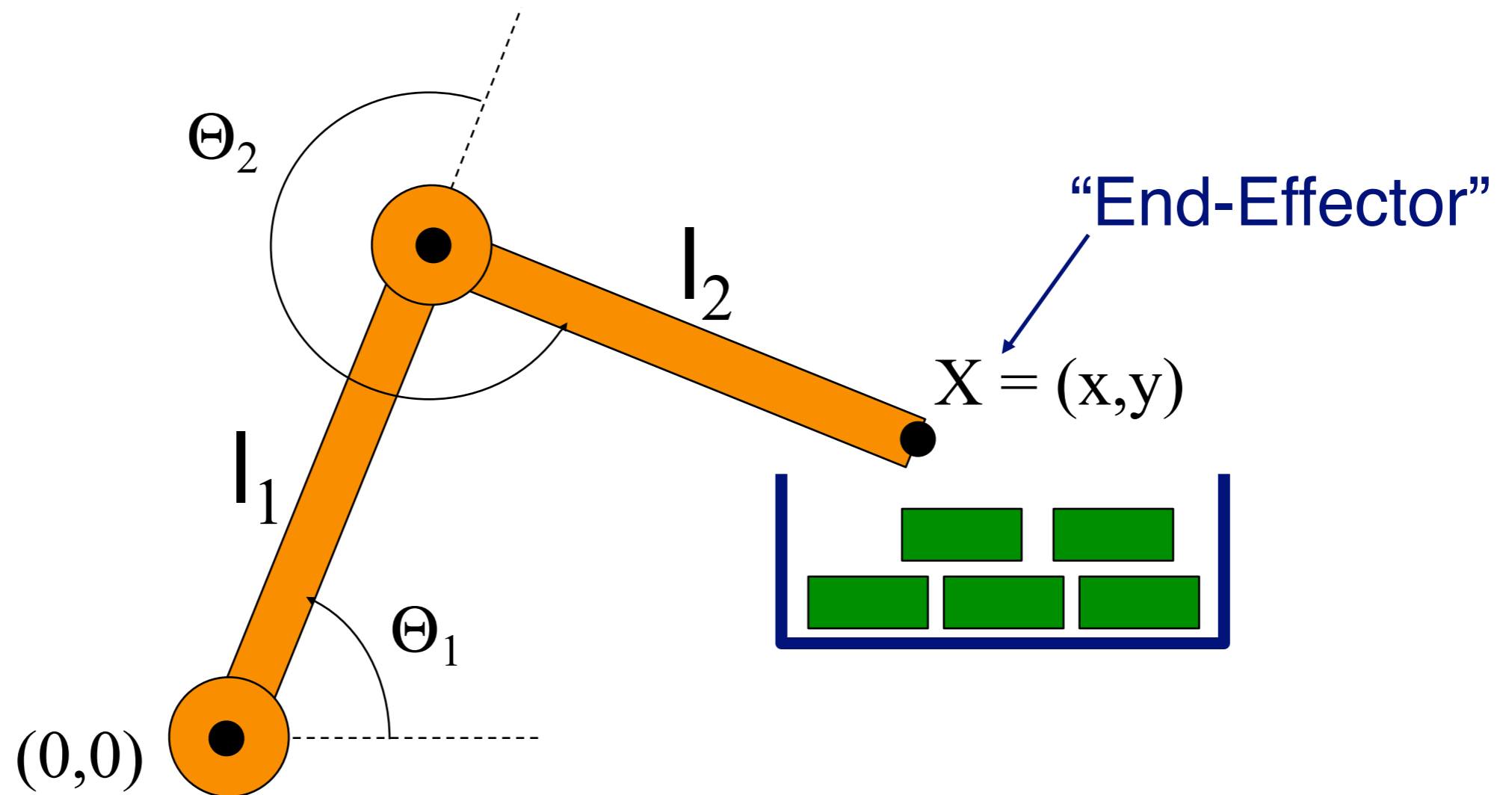
$$\Theta_2(0) = 250^\circ$$

$$\frac{d\Theta_1}{dt} = 1.2$$

$$\frac{d\Theta_2}{dt} = -0.1$$

# Example: 2-Link Structure

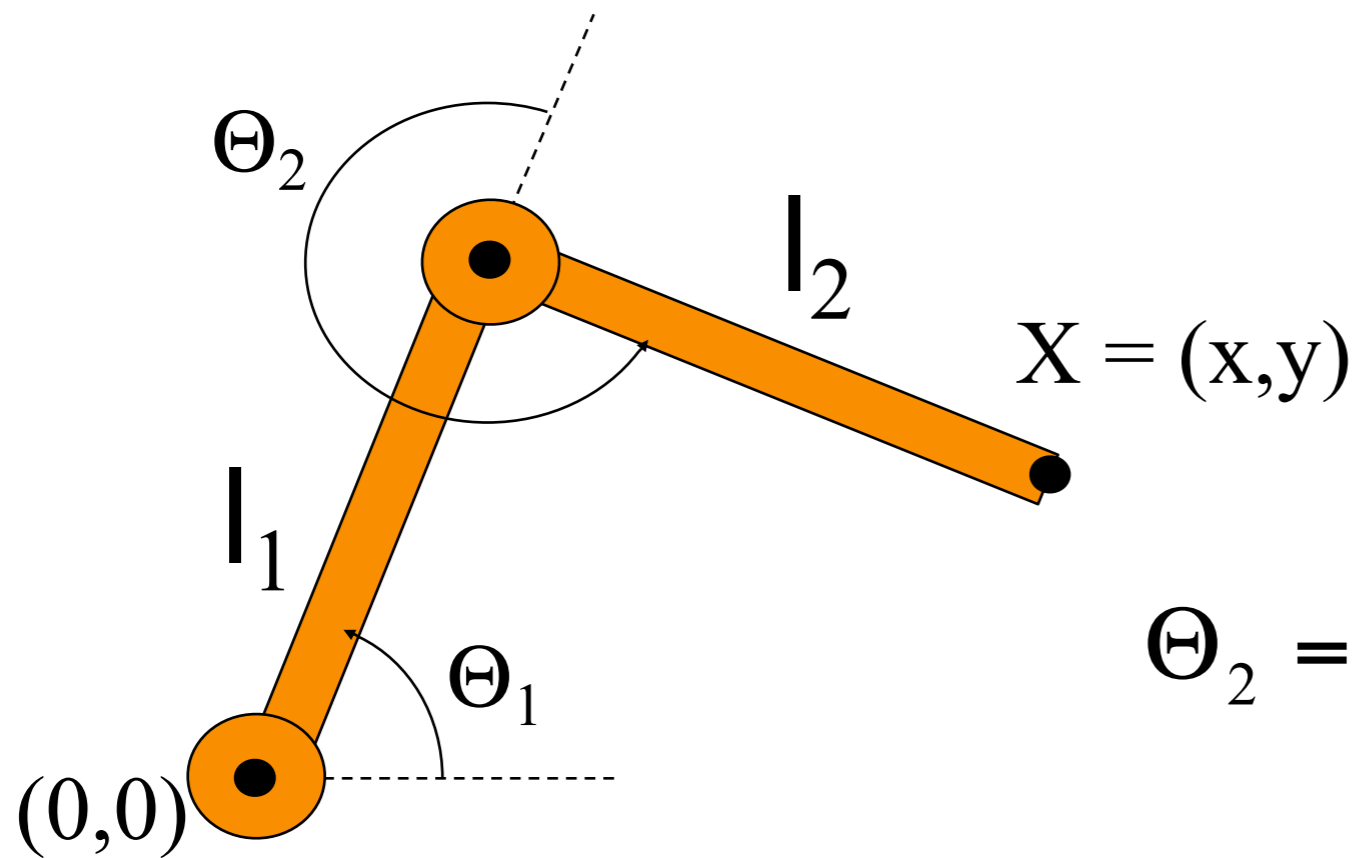
- What if animator knows position of “end-effector”





# Inverse Kinematics

- Animator specifies end-effector positions:  $X$
- Computer finds joint angles:  $\Theta_1$  and  $\Theta_2$ :

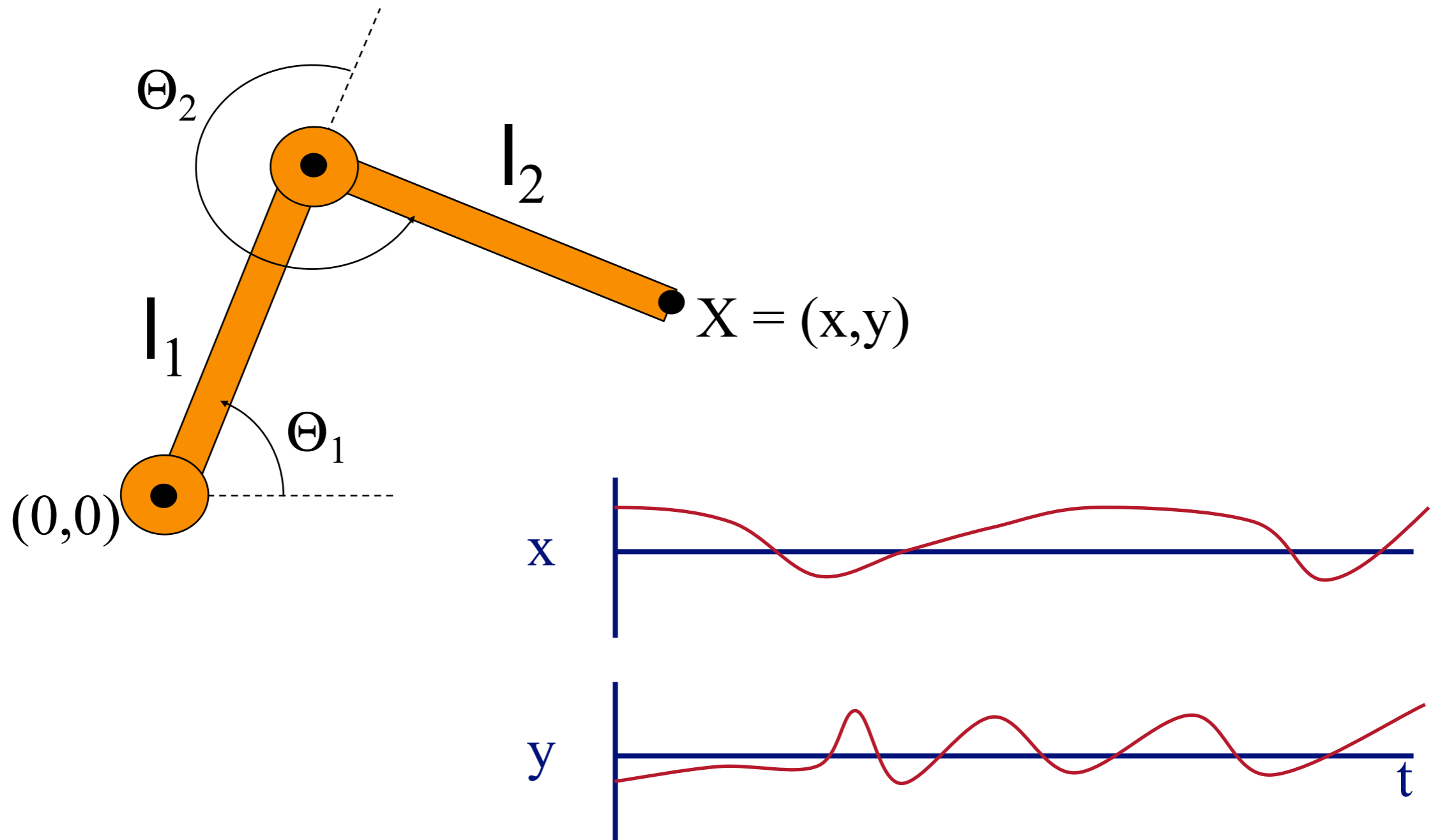


$$\Theta_2 = \cos^{-1} \left( \frac{x^2 + y^2 - l_1^2 - l_2^2}{2l_1l_2} \right)$$

$$\Theta_1 = \frac{-(l_2 \sin(\Theta_2)x + (l_1 + l_2 \cos(\Theta_2))y)}{(l_2 \sin(\Theta_2))y + (l_1 + l_2 \cos(\Theta_2))x}$$

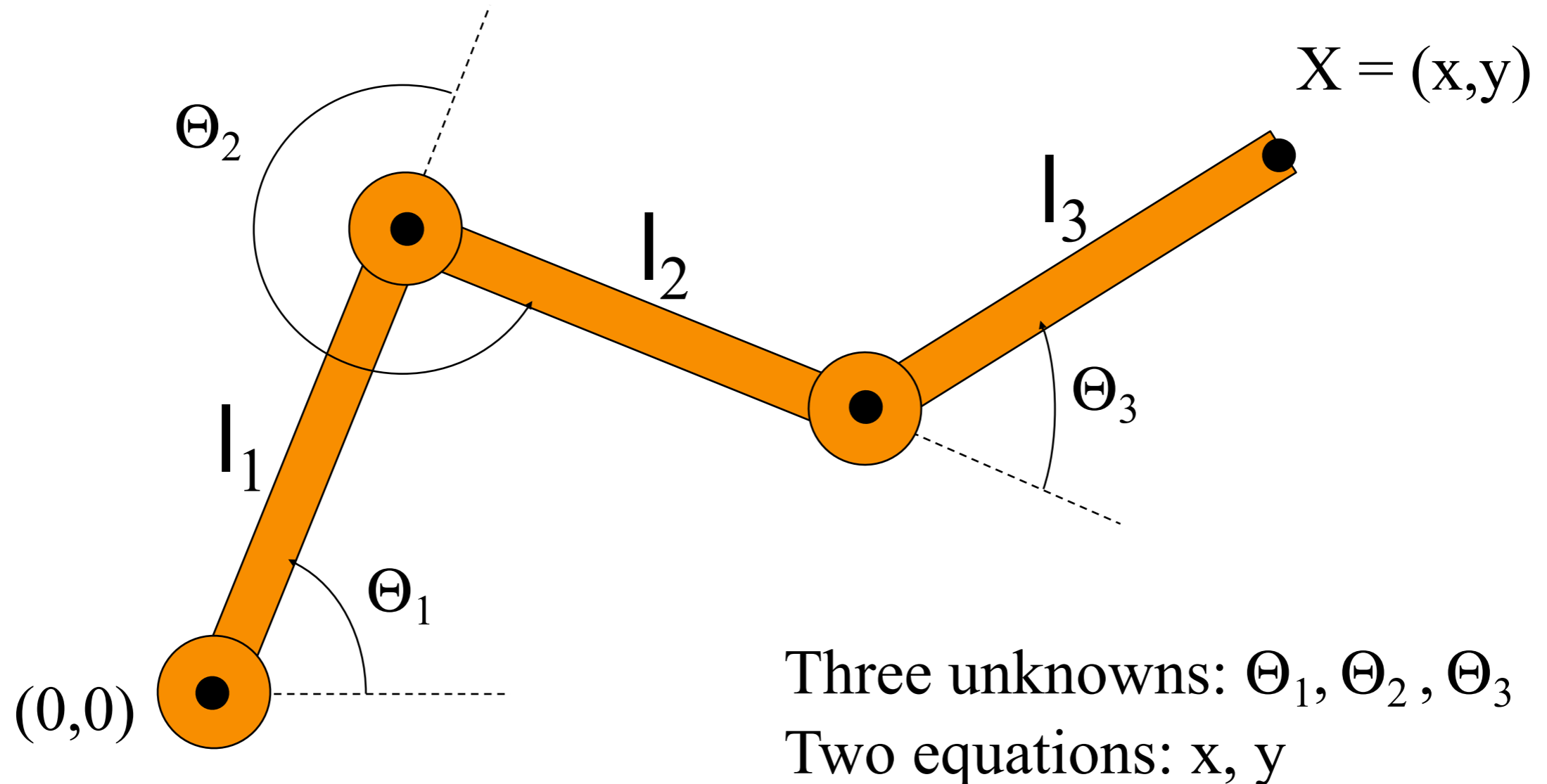
# Inverse Kinematics

- End-effector positions can be specified by splines



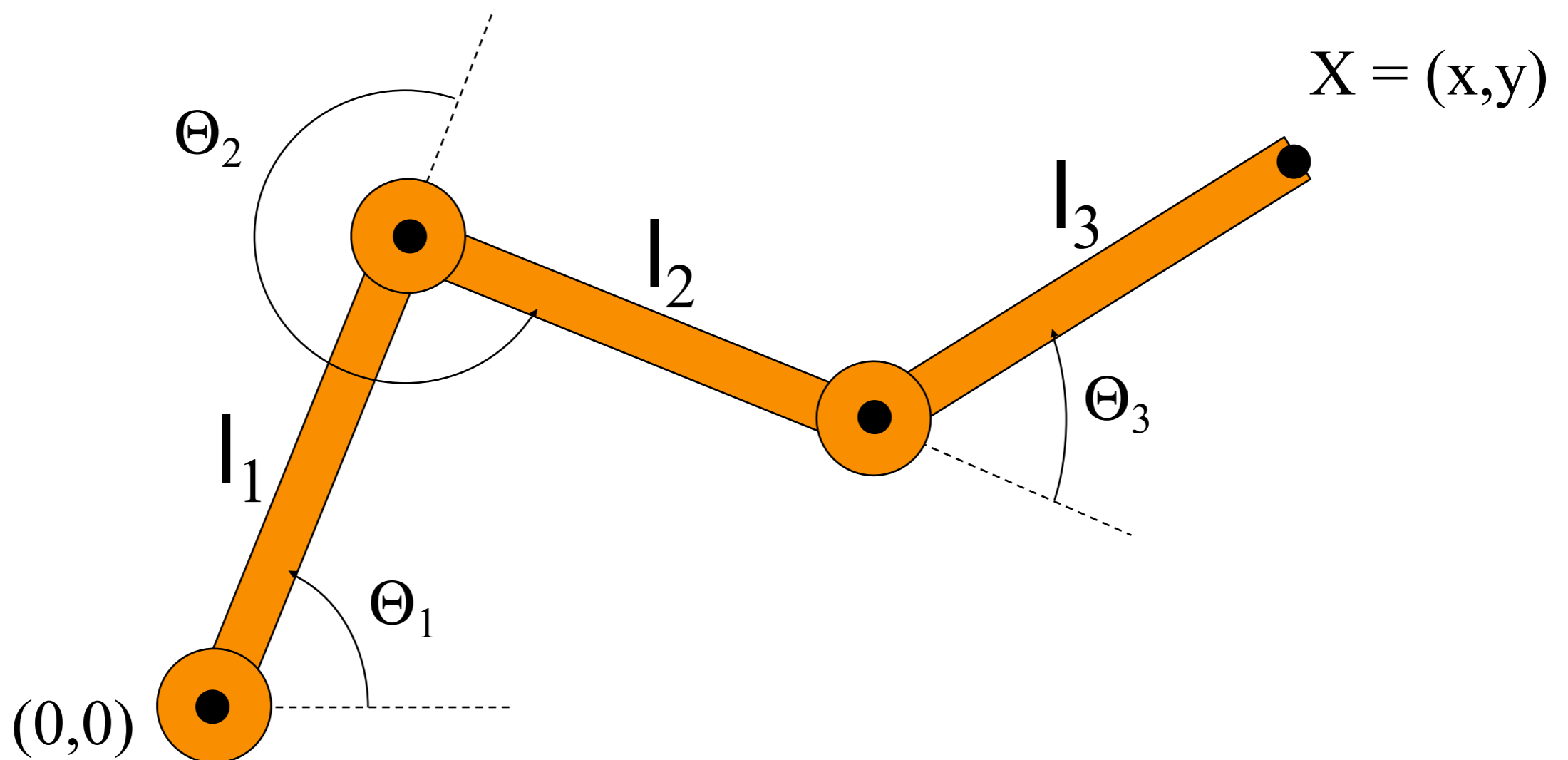
# Inverse Kinematics

- Problem for more complex structures
  - System of equations is usually under-defined
  - Multiple solutions



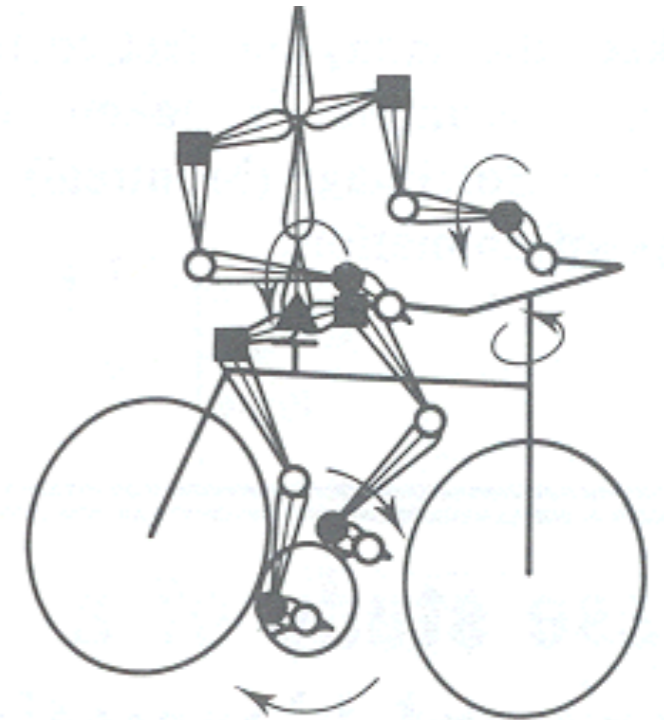
# Inverse Kinematics

- Solution for more complex structures:
  - Find best solution (e.g., minimize energy in motion)
  - Non-linear optimization



# Summary of Kinematics

- Forward kinematics
  - Specify conditions (joint angles)
  - Compute positions of end-effectors
- Inverse kinematics
  - “Goal-directed” motion
  - Specify goal positions of end effectors
  - Compute conditions required to achieve goals



Inverse kinematics provides easier specification for many animation tasks, but it is computationally more difficult

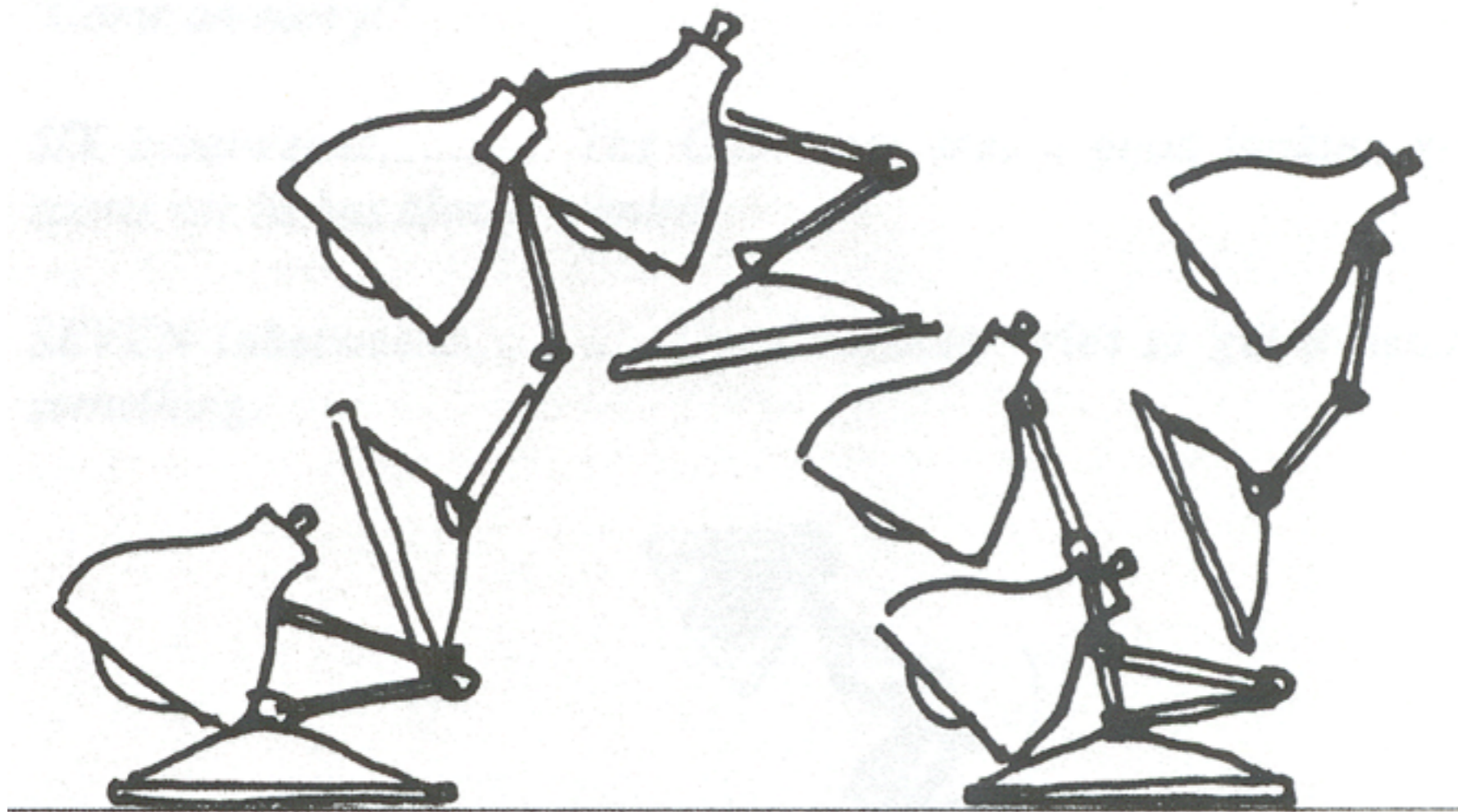


# Overview

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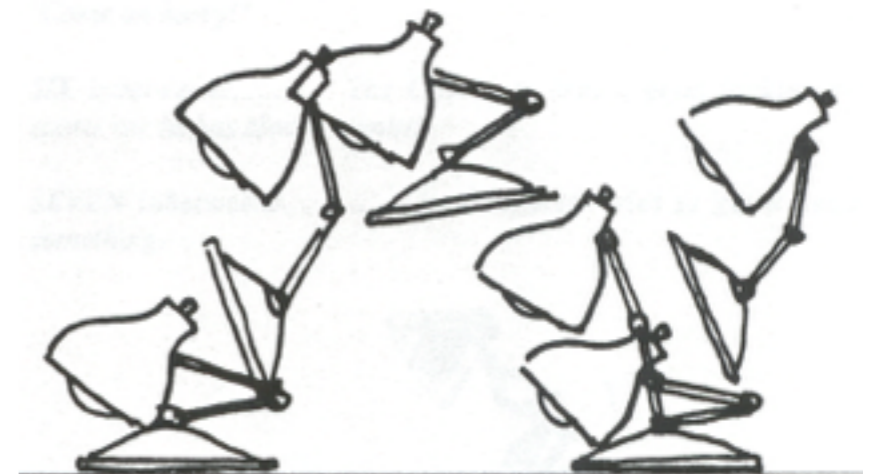
# Dynamics

- Simulation of physics insures realism of motion



# Spacetime Constraints

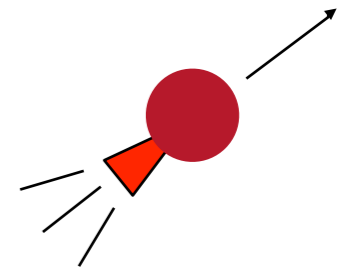
- Animator specifies constraints:
  - What the character's physical structure is
    - » e.g., articulated figure
  - What the character has to do
    - » e.g., jump from here to there within time  $t$
  - What other physical structures are present
    - » e.g., floor to push off and land
  - How the motion should be performed
    - » e.g., minimize energy



# Spacetime Constraints

- Computer finds the “best” physical motion satisfying constraints
- Example: particle with jet propulsion
  - $x(t)$  is position of particle at time  $t$
  - $f(t)$  is the directional force of jet propulsion at time  $t$
  - Particle’s equation of motion is:

$$mx'' - f - mg = 0$$



- Suppose we want to move from  $a$  to  $b$  within  $t_0$  to  $t_1$  with minimum jet fuel:

$$\text{Minimize } \int_{t_0}^{t_1} |f(t)|^2 dt \quad \text{subject to } x(t_0) = a \text{ and } x(t_1) = b$$

# Spacetime Constraints

- Discretize time steps:

$$x'_i = \frac{x_i - x_{i-1}}{h}$$
$$x''_i = \frac{x_{i+1} - 2x_i + x_{i-1}}{h^2}$$

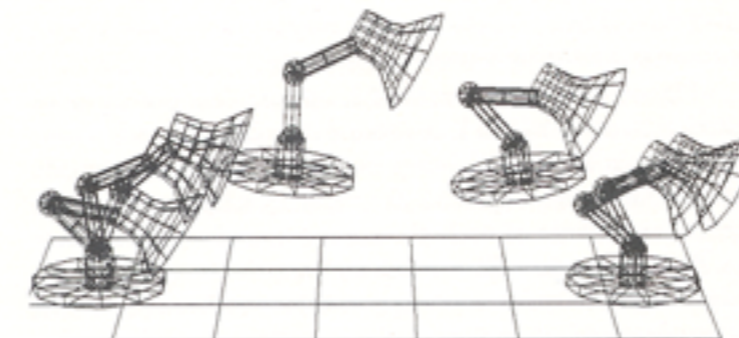
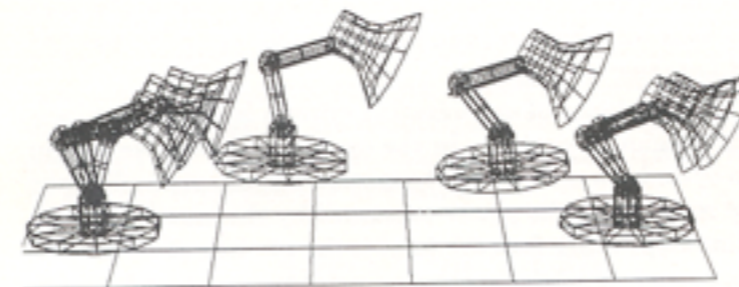
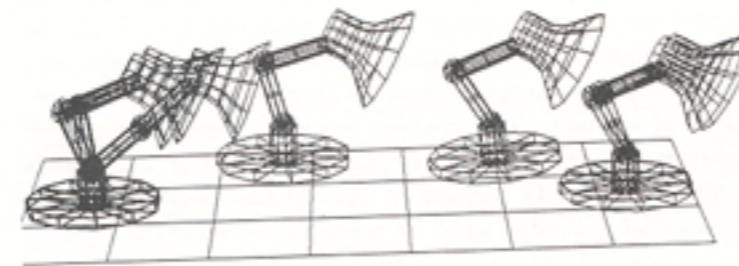
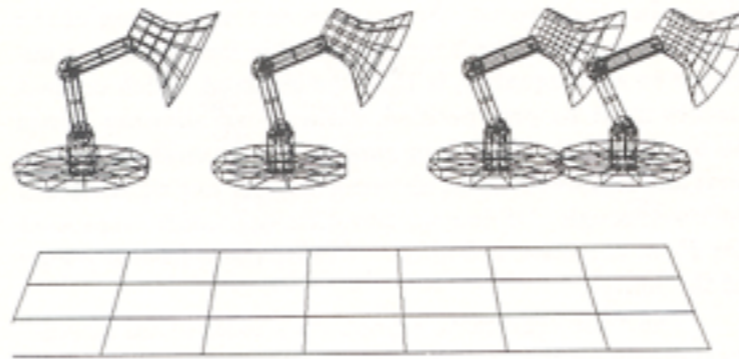
$$m \left( x''_i = \frac{x_{i+1} - 2x_i + x_{i-1}}{h^2} \right) - f_i - mg = 0$$

Minimize  $h \sum_i |f_i|^2$  subject to  $x_0 = a$  and  $x_1 = b$



# Spacetime Constraints

- Solve with iterative optimization methods

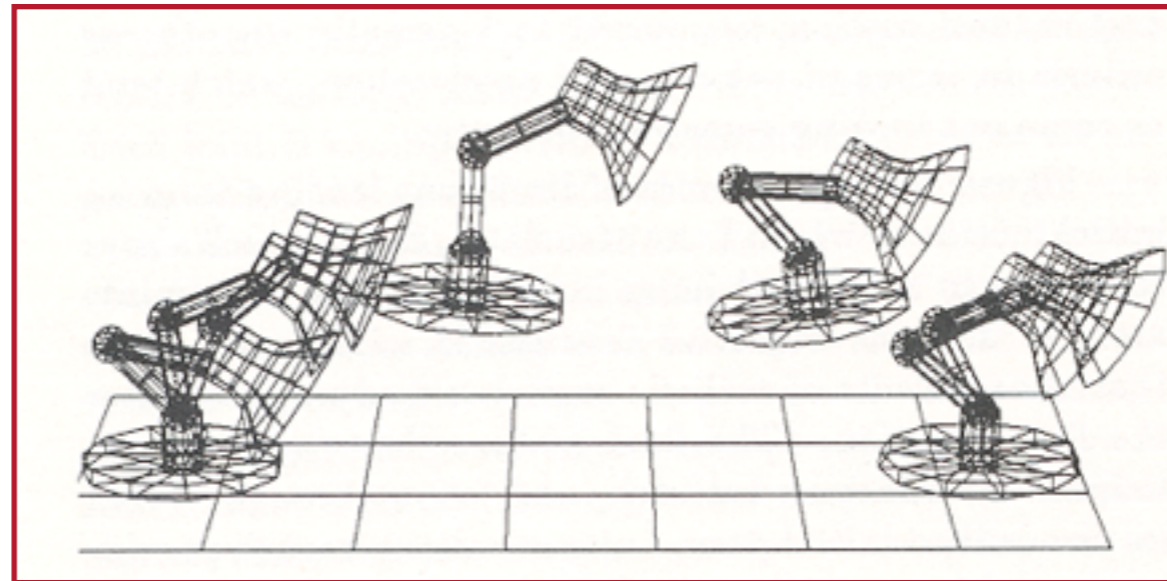


# Spacetime Constraints

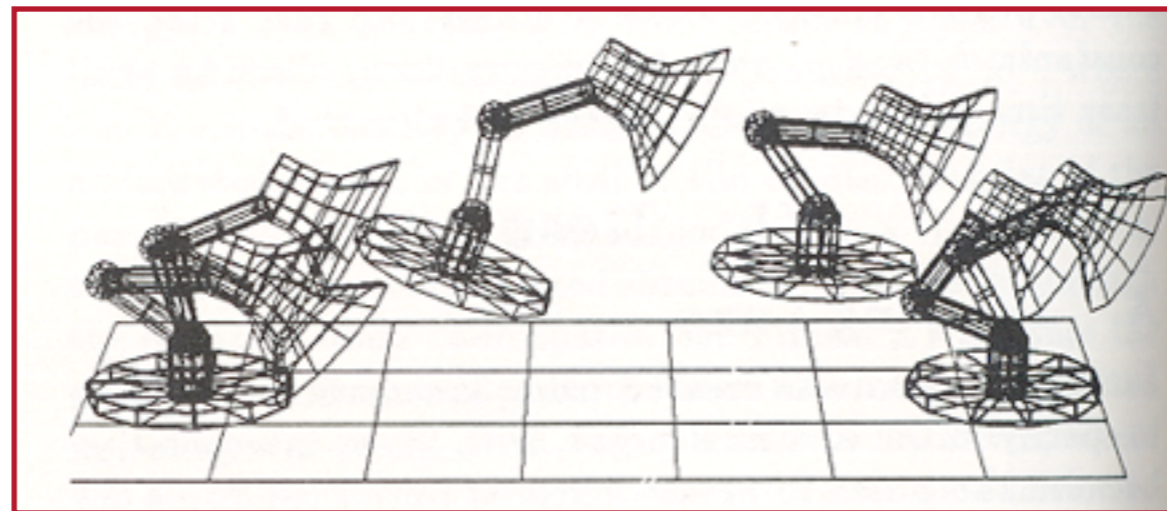
- Advantages:
  - Free animator from having to specify details of physically realistic motion with spline curves
  - Easy to vary motions due to new parameters and/or new constraints
- Challenges:
  - Specifying constraints and objective functions
  - Avoiding local minima during optimization

# Spacetime Constraints

- Adapting motion:



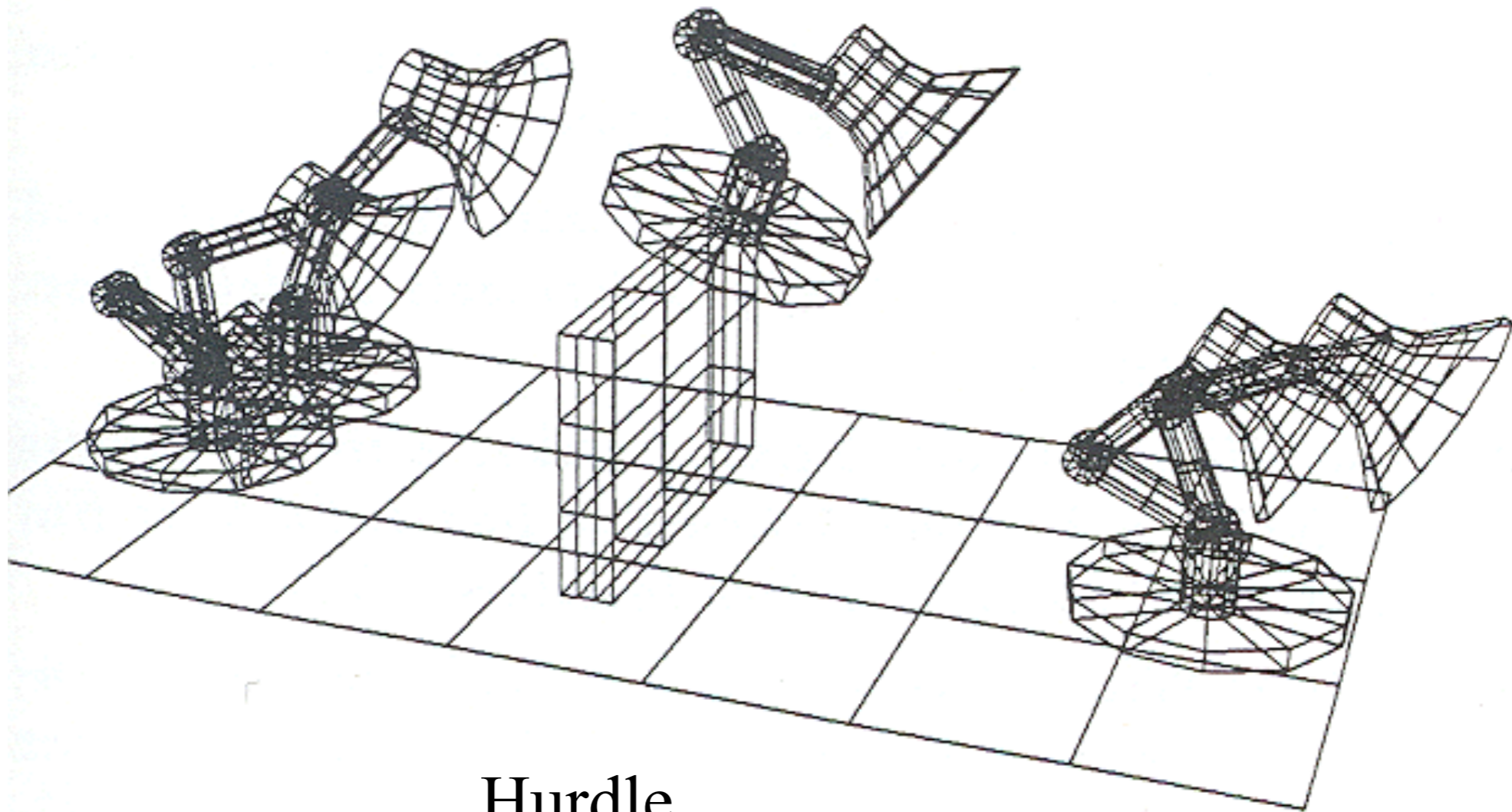
Original Jump



Heavier Base

# Spacetime Constraints

- Adapting motion:

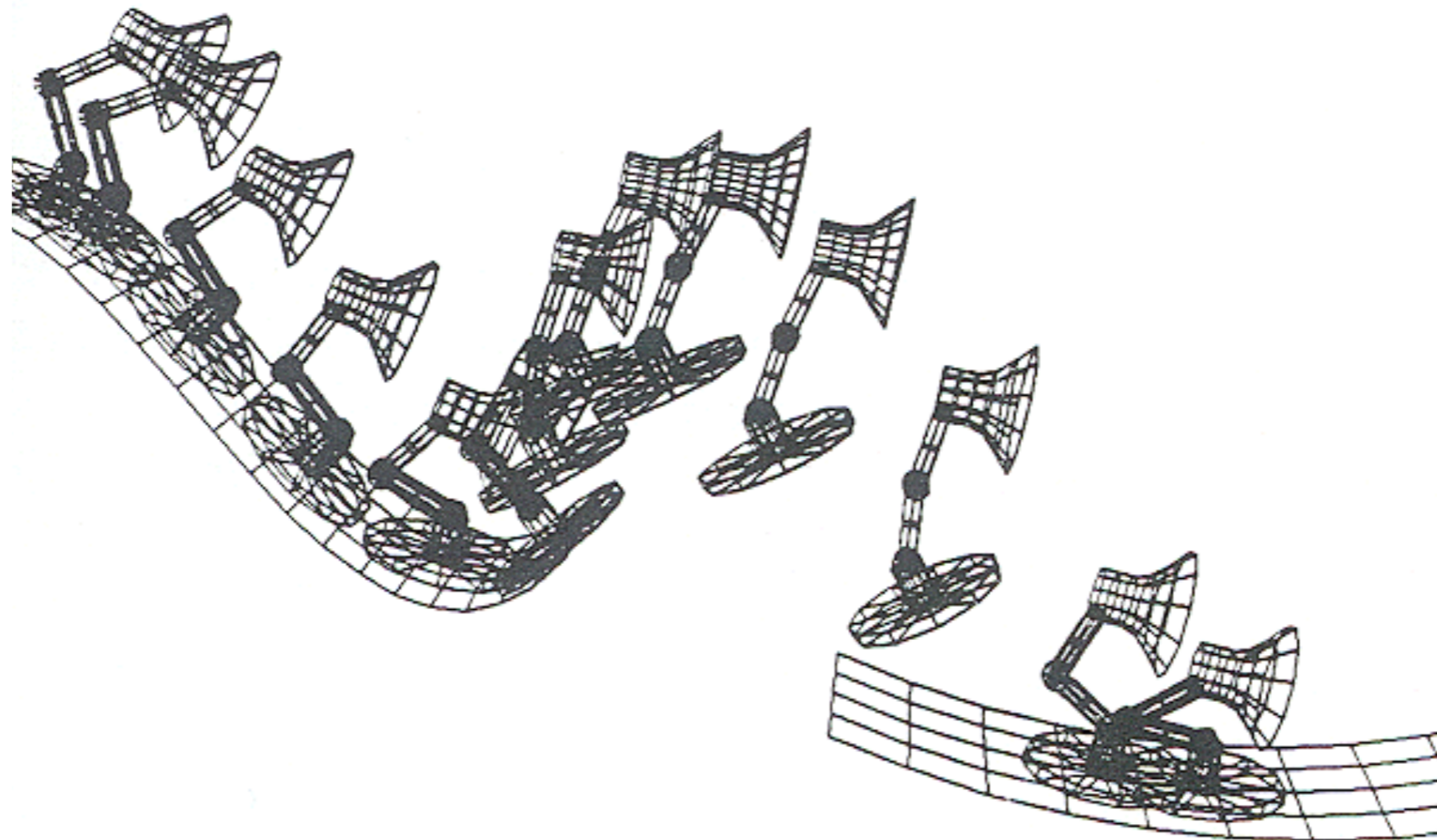


Hurdle



# Spacetime Constraints

- Adapting motion:



Ski Jump



# Dynamics

- Other physical simulations:
  - Rigid bodies
  - Soft bodies
  - Cloth
  - Liquids
  - Gases
  - etc.



Hot Gases  
*(Foster & Metaxas '97)*



Cloth  
*(Baraff & Witkin '98)*

# Summary

- Principles of animation
- Keyframe animation
- Articulated figures